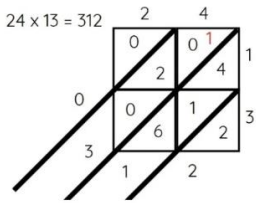


## Integers, Place Value and Decimals

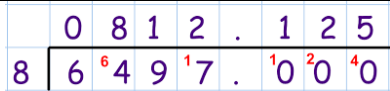
### Number Skills

1.	Addition	To find the sum or total of two or more numbers.
2.	Subtraction	To find the difference between two numbers.
3.	Multiplication	Repeated addition of a number. Also called 'product'
4.	Division	The process of calculating the number of times one number is contained in another.
5.	Divisible	Can be divided by a number without a remainder.

### Multiplication methods

6.	Lattice	<div><div>24 x 13 = 312</div><div></div></div>												
7.	Grid	<div><div>Eg) 574 x 29</div><div><table><tr><td></td><td>500</td><td>70</td><td>4</td></tr><tr><td>20</td><td>10000</td><td>1400</td><td>80</td></tr><tr><td>9</td><td>4500</td><td>630</td><td>36</td></tr></table><div><div>11480</div><div>+ 5166</div><div>-----</div><div>16646</div><div>-----</div><div>Finished!</div></div></div></div>		500	70	4	20	10000	1400	80	9	4500	630	36
	500	70	4											
20	10000	1400	80											
9	4500	630	36											
8.	Column	<div><div><div><div><div><div><div>×</div><div>36</div></div><div><div>15</div></div></div></div><div><div>30</div><div>60</div><div>150</div><div>300</div></div><div><div>-----</div><div>540</div></div></div><div><div>30</div><div>10</div></div><div><div>6</div><div>5</div></div><div><div>6</div><div>5</div></div><div><div>(6 x 5)</div><div>(6 x 10)</div><div>(30 x 5)</div><div>(30 x 10)</div></div></div></div>												

### Division methods

9.	Short	<p>e.g. <math>6497 \div 8</math></p> 
----	-------	---

10.

Long

e.g.  $13032 \div 24$

543

1 - 24

2 - 48

3 - 72

4 - 96

5 - 120

6 - 144

7 - 168

8 - 192

9 - 216

24

13032

- 120

103

- 96

72

- 72

00

Times Tables

x	1	2	3	4	5	6	7	8	9	10
1	1	2	3	4	5	6	7	8	9	10
2	2	4	6	8	10	12	14	16	18	20
3	3	6	9	12	15	18	21	24	27	30
4	4	8	12	16	20	24	28	32	36	40
5	5	10	15	20	25	30	35	40	45	50
6	6	12	18	24	30	36	42	48	54	60
7	7	14	21	28	35	42	49	56	63	70
8	8	16	24	32	40	48	56	64	72	80
9	9	18	27	36	45	54	63	72	81	90
10	10	20	30	40	50	60	70	80	90	100

Divisibility Rules

11.

A number is divisible

by:

if:

2

The last digit is divisible by 2

3

The sum of the digits is divisible by 3

4

The number made by the last two digits is divisible by 4

5

The last digit is 5 or 0

6

The number is divisible by 2 and 3

8

The number made by the last 3 digits is divisible by 8

9

The sum of its digits is divisible by 9

10

The last digit is 0.

12.

Place value

The value of a digit based on its place in a number

Millions

Hundred Thousands

Ten Thousands

Thousands

Hundreds

Tens

Ones

Decimal point ↓

Tenths

Hundredths

Thousandth

Ten-Thousandths

Hundred-Thousandth

Millionths

Whole part

•

Decimal part

13.	Digit	A single symbol used to make a number	
		0, 1, 2, 3, 4, 5, 6, 7, 8, 9 are the ten digits we use every day.	
14.	Integer	A whole number that is can be positive, negative or zero.	
15.	Negative number	A number that is less than zero.	
16.	Negative number rules	When multipllying or dividing with numbers that include negative numbers to following applies:	<div> <math>\begin{array}{ccccccc} (+) &amp; \times &amp; (+) &amp; = &amp; (+) \\ (+) &amp; \times &amp; (-) &amp; = &amp; (-) \\ (-) &amp; \times &amp; (+) &amp; = &amp; (-) \\ (-) &amp; \times &amp; (-) &amp; = &amp; (+) \end{array}</math> </div> <div> <math>\begin{array}{ccccccc} (+) &amp; \div &amp; (+) &amp; = &amp; (+) \\ (+) &amp; \div &amp; (-) &amp; = &amp; (-) \\ (-) &amp; \div &amp; (+) &amp; = &amp; (-) \\ (-) &amp; \div &amp; (-) &amp; = &amp; (+) \end{array}</math> </div>
17.	Ascending order	A set of numbers arranged from smallest to biggest.	
18.	Descending order	A set of numbers arranged from biggest to smallest.	
19.	Decimal	A number with a decimal point in it, which can be negative or positive.	
20.	Terminating decimal	A decimal that has digits that end.	0.25 (it has two decimal digits) 3.0375 (it has four decimal digits)
21.	Recurring decimal	A decimal with a digit or groups of digits that repeat forever.	$\frac{1}{3} = 0.333... = 0.\dot{3} = 0.\overline{3}$ <i>Fraction</i> <i>Ways to show recurring decimals</i>
22.	Decimal place	The number of digits after the decimal point	
23.	Rounding	Changing a number to a simpler, easy to use value.	
24.	Approximate	An easier figure to use close to the value.	
25.	Significant figure	The digits of a number that express a size to a given degree of accuracy	
Rounding to decimal places			

26.	<ul style="list-style-type: none"> <li>Count the number of decimal places you need</li> <li>Look at the number directly to the right of that digit to decide if it rounds up or down</li> <li>5 or more means it rounds up; 4 or less means it rounds down</li> </ul>	
27.	e.g. 256.1873	<div>256.1   873</div> <div>To 1 d.p. is 256.2</div> <div>256.18   73</div> <div>To 2 d.p. is 256.19</div> <div>256.187   3</div> <div>To 3 d.p. is 256.187</div>

#### Rounding large numbers to significant figures

28.	<ul style="list-style-type: none"> <li>Count the number of digits you need from the left</li> <li>Look at the number to the right of the digit to decide if it rounds up or down</li> <li>5 or more means it rounds up; 4 or less means it rounds down</li> <li>Replace remaining digits with zeros as placeholders</li> </ul>	
29.	e.g. 256. 1873	<div>2   56.1873</div> <div>To 1 s.f. is 300</div> <div>25   6.1873</div> <div>To 2 s.f. is 260</div> <div>256   .1873</div> <div>To 3 s.f. is 256</div>



#### Rounding small numbers to significant figures

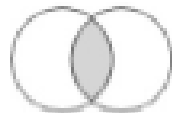
30.	<ul style="list-style-type: none"> <li>Zeros are not significant until after the first non-zero term</li> <li>Find the first non-zero term and count the number of digits you need from there</li> <li>Look at the number directly to the right of that digit to decide if it rounds up or down</li> <li>5 or more means it rounds up; 4 or less means it rounds down</li> </ul>	
31	e.g. 0.0023681	<div>0.002   3681</div> <div>To 1 s.f. is 0.002</div> <div>0.0023   681</div> <div>To 2 s.f. is 0.0024</div> <div>0.00236   81</div> <div>To 3 s.f. is 0.00237</div>

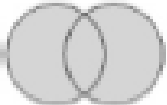
#### Inequality notation

32.	=	Equal to
33.	≠	Not equal to
34.	<	Less than
35.	>	Greater than
36.	≤	Less than or equal to
37.	≥	Greater than or equal to

## Indices, powers and roots

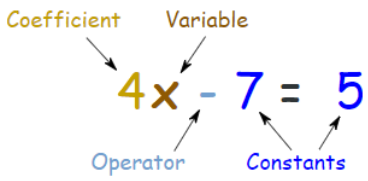
		Symbols and words to show how to combine numbers.			
38.	Operations	$\times$	Multiply	$+$	Add
		$\div$	Divide	$-$	Subtract
39.	Order of operations	The order in which operations should be carried out.		B I DM AS	Brackets Indices Divide and Multiply Add and Subtract
40.	Inverse operations	The operation used to reverse the original operation			
		$+$ and $-$ are inverse		$\times$ and $\div$ are inverse	
		Finding the square root is the inverse of finding the square of a number.			
		Finding the cube root is the inverse of finding the cube of a number.			
41.	Square numbers	The product of a number multiplied by itself.		4	 $2^2$ or $2 \times 2 = 4$
42.	Cube numbers	The product of multiplying a number by itself three times		$2^3 = 2 \times 2 \times 2 = 8$ 	
43.	Square root	A value that can be multiplied by itself to give the original number		$\sqrt{1} = \pm 1$ $\sqrt{81} = \pm 9$ $\sqrt{4} = \pm 2$ $\sqrt{100} = \pm 10$ $\sqrt{9} = \pm 3$ $\sqrt{121} = \pm 11$ $\sqrt{16} = \pm 4$ $\sqrt{144} = \pm 12$ $\sqrt{25} = \pm 5$ $\sqrt{169} = \pm 13$ $\sqrt{36} = \pm 6$ $\sqrt{196} = \pm 14$ $\sqrt{49} = \pm 7$ $\sqrt{225} = \pm 15$ $\sqrt{64} = \pm 8$	
44.	Cube root	A value that can be multiplied by itself three times to give the original number		$\sqrt[3]{1} = 1$ $\sqrt[3]{216} = 6$ $\sqrt[3]{8} = 2$ $\sqrt[3]{343} = 7$ $\sqrt[3]{27} = 3$ $\sqrt[3]{512} = 8$ $\sqrt[3]{64} = 4$ $\sqrt[3]{729} = 9$ $\sqrt[3]{125} = 5$ $\sqrt[3]{1000} = 10$	
45.	Index	A small number to the upper right of a base number that shows how many times the base number is multiplied by itself.			
46.	Power	Another word for an index.			

47.	Indices	The plural of index.		
48.	Index form	A number written to the power of an index.		
Laws of indices				
49.	Multiplying	Add the powers	$x^7 \times x^6 = x^{13}$	
50.	Dividing	Subtract the powers	$x^5 \div x^6 = x^{-1}$	
51.	Brackets	Multiply the powers	$(x^2)^3 = x^6$	
52.	Power of 0	Always = 1	$x^0 = 1$	
53.	Negative	Means “1 over”	$x^{-n} = \frac{1}{x^n}$	
54.	Unit Fraction	Means root	$x^{\frac{1}{n}} = \sqrt[n]{x}$	
55.	Fractional	Means root and bracket	$x^{\frac{a}{n}} = (\sqrt[n]{x})^a$	
Factors, multiples and primes				
56.	Multiple	The result of multiplying a number by an integer.		
57.	Factor	A number that divides into another number without a remainder.		
58.	Remainder	An amount left over after dividing.		
59.	Prime number	A number with exactly two factors; 1 and itself.		
		2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97.		
60.	Product	The answer when two or more numbers are multiplied together.		
61.	Prime factor decomposition	Writing a number as a product of its prime factors.		<div><div><div>60</div><div>2</div><div>30</div><div>2</div><div>15</div><div>3</div><div>5</div><div>5</div><div>1</div></div><div><math>60 = 2 \times 2 \times 3 \times 5</math> <math>60 = 2^2 \times 3 \times 5</math></div></div> <div><div><div>72</div><div>2</div><div>36</div><div>2</div><div>18</div><div>2</div><div>9</div><div>3</div><div>3</div><div>3</div><div>1</div></div><div><math>72 = 2 \times 2 \times 2 \times 2 \times 3 \times 3</math> <math>72 = 2^4 \times 3^2</math></div></div>
62.	Highest common factor	HCF	The highest number that divides exactly into two or more numbers.	<div>e.g. the HCF of 12 and 8 is 4</div> <div></div>

63.	Lowest common multiple	LCM	The smallest positive integer that is a multiple of two or more numbers.	e.g. the LCM of 12 and 8 is 24	
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## Algebra: the basics

### Definitions

1.	Variable	A letter representing a varying or unknown quantity.	
2.	Coefficient	A number which multiplies a variable e.g. 4 is the coefficient in $4a$	
3.	Term	One part of an expression/equation/formula	e.g. $4c$ $\frac{w}{5}$
		Can involve multiplying and dividing coefficients and variables	
		Separated from other terms by addition and subtraction	
4.	Like terms	Terms that have the same variable but have different coefficients	e.g. $c + 4c$ are like terms $c^2$ and $c^3$ are not like terms
5.	Constant	A fixed value.	
		A number on its own or sometimes a letter such as $a$ , $b$ or $c$ to represent a fixed number.	
6.	Expression	One or a group of terms.	e.g. $3y - 3$ $3y^2 + y^3$
		Can include variables, constants, operators and grouping symbols.	
		No 'equals' sign	
7.	Equation	Contains an 'equals' sign, =	e.g. $3y - 3 = 12$
		Has at least one variable	
8.	Formula	A special type of equation that shows the relationship between a set of variables	
9.	Formulae	Plural of 'formula'	
10.	Identity	An equation that is true no matter what values are chosen, $\equiv$	e.g. $3y \equiv 2y - y$ for any value of $y$ .
11.	Subject	The variable on its own on one side of the equals sign.	
12.	Substitute	Replace a variable with a number.	$a = 3, b = 2$ and $c = 5$ .  Find: 1. $2a = 2 \times 3 = 6$ 2. $3a - 2b = 3 \times 3 - 2 \times 2 = 5$ 3. $7b^2 - 5 = 7 \times 2^2 - 5 = 23$
13.	Simplify	Minimising the size of an expression	

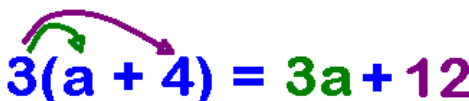
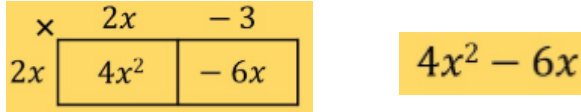


14.	Factorise	Splitting an expression into a product of factors
15.	Expand	Removing brackets by using multiplication
16.	Solve	Find the value of an unknown

### Algebraic Notation

17.	Adding like terms	Add the coefficients	$b + 2b = 3b$
18.	Subtracting like terms	Subtract the coefficients	$5b - 4b = b$
19.	Multiplying like terms	If the base is the same, add the powers	$b \times b = b^2$
20.	Dividing terms	If the base is the same, subtract the powers	$b^5 \div b^2 = b^3$
21.	Adding different terms	Cannot combine if the terms are different.	$b + 2c = b + 2c$
22.	Subtracting different terms	Cannot combine if the terms are different.	$3c - 4 = 3c - 4$
23.	Multiplying different terms	Combine with no '×' sign	$d \times e = de$
24.	Multiplying different terms with coefficients	Combine with no '×' sign, multiply the coefficients	$2d \times 3e = d6e$
25.	Dividing different terms	Write as fractions with no '÷' sign	$3d \div e = \frac{3d}{e}$
26.	Dividing different terms with coefficients	Write as fractions with no '÷' sign, simplify the coefficients where possible.	$14d \div 7e = \frac{2d}{e}$

### Expanding (single brackets)

27.	Multiply all the terms inside the bracket, by the term on the outside.		
28.			

### Factorising (single brackets)

29.	<ul style="list-style-type: none"> <li>Find the highest common factor of the terms</li> <li>This goes outside the bracket</li> <li>Divide each term by the factor to get the new terms inside the bracket</li> <li>Always check by expanding your bracket</li> </ul>	$2x + 4y$ $2(x + 2y)$ $5x^2y - 10xy$ $5xy(x - 2)$
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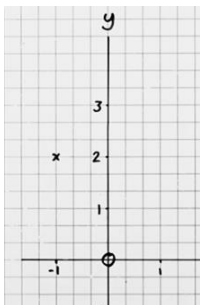
### Expressions

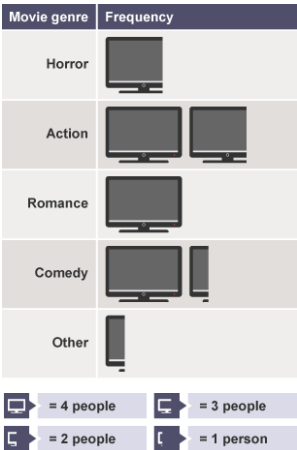
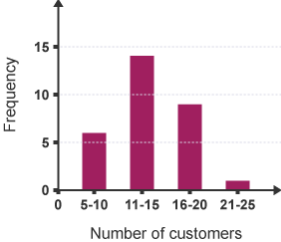
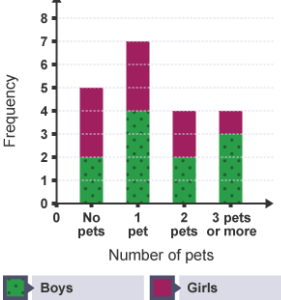
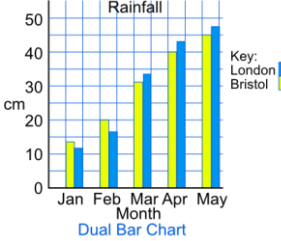
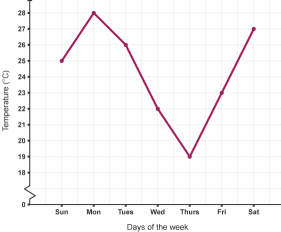
30.	Linear	Can be represented by a straight line	e.g. $2x + 2$
		No indices above 1	
31.	Quadratic	An expression where the highest index is 2	e.g. $2x^2 + 2x + 2$

## 3a. TABLES

1	TYPES OF DATA					
1a	Qualitative Data	Non-numerical data			i.e. Colour of car	
1b	Quantitative Data	Numerical data			i.e. House number	
1c	Discrete Data	Numerical data that <u>CANNOT</u> be shown in decimals			i.e. Number of children in a class	
1d	Continuous Data	Numerical data that <u>CAN</u> be shown in decimals			i.e. The heights of children in a class	
1e	Grouped Data	Numerical data given in intervals			i.e. Year group ranges: Year 7-9    Year 10-11    Year 12-13	
2	Data Collection	Three Columns: <ul style="list-style-type: none"><li>• Data values</li><li>• Tally</li><li>• Frequency (how many)</li></ul>	Colour of Car	Tally	Frequency	
			Red	IIII	4	
			White	IIII	5	
			Grey	III	3	
			Black	IIII III	8	
			Blue	IIII I	6	
3	Mode	Most popular (i.e. most common colour of car is Black)				
4a	24-hour clock	15:30	Uses hours 00 (Midnight) to 23 (11 in the evening)			
4b	12-hour clock	03:30 pm	Uses hours 01 to 12 with morning (AM) and afternoon/evening (PM)			
5	Two-Way Tables		Boys	Girls	TOTAL	Two-way tables are a way of sorting data with two categories.
		Pet	9	4	13	
		No Pet	2	5	7	
		TOTAL	11	9	20	

## 3b. Charts and Graphs

6	Plotting Points	<p>Co-ordinates show an exact position</p> <p><math>(x, y)</math></p>	
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7	Pictograms	 <p>Movie genre    Frequency</p> <p>Horror    [Icon]</p> <p>Action    [Icon] [Icon]</p> <p>Romance    [Icon]</p> <p>Comedy    [Icon] [Icon]</p> <p>Other    [Icon]</p> <p>[Icon] = 4 people    [Icon] = 3 people [Icon] = 2 people    [Icon] = 1 person</p>	<p>Used to show frequencies</p> <p>Pictures and images used to represent frequency A key at the bottom helps you interpret the diagram</p>
8a	Bar Charts	 <p>Frequency</p> <p>Number of customers</p>	<p>Frequency on the vertical axis, and categories along the horizontal axis.</p> <p>Used to compare frequencies</p>
8b	Composite Bar Chart	 <p>Frequency</p> <p>Number of pets</p> <p>Boys    Girls</p>	<p>Frequency on the vertical axis, and categories along the horizontal axis.</p> <p>Two shades used to show difference in proportion between sub-groups (i.e. gender)</p> <p>Used to compare frequencies within sub-groups</p>
8c	Comparative Bar Chart	 <p>Rainfall</p> <p>cm</p> <p>Month</p> <p>Dual Bar Chart</p> <p>Key: London Bristol</p>	<p>Frequency on the vertical axis, and categories along the horizontal axis.</p> <p>Bars are next to each other and used to show difference in frequency between sub-groups (i.e. gender)</p> <p>Used to compare frequencies within sub-groups</p>
9	Line Graph	 <p>Temperature (°C)</p> <p>Days of the week</p>	<p>A line graph is used to show a change or relationship between two variables.</p> <p>Once the points are plotted, they are joined with straight lines.</p>

10	Time-Series		<p>A time-series graph plots frequencies (vertical) axis against time (horizontal).</p> <p>It is used to spot trends over time.</p> <p>Time could be: weeks, months, quarters (3 months), years</p>
11	Stem & Leaf Diagrams:	<p>Key: 1   1 = 11 marks</p> <pre> 0   9 1   1 6 7 8 2   1 2 7 7 8 8 9 3   0 0 1 5 6 7 8 9 4   0 1 2 5 </pre>	<p>A stem and leaf diagram shows numbers in a table format. It can be a useful way to organise data to find the median, mode and range of a set of data.</p> <p>Only one digit is allowed to be a 'leaf'</p> <p>There should be a key to help you interpret the diagram</p>

3c. Pie Charts

12

Pie Charts

A pie chart is a chart represented by a circle. It shows the proportion of each group at a glance.

People travelling in a vehicle	Frequency	Calculation	Angle
1 person	120	$\frac{120}{180} \times 360^\circ$	240°
2 people	40	$\frac{40}{180} \times 360^\circ$	80°
3 people	13	$\frac{13}{180} \times 360^\circ$	24°
4 people	5	$\frac{5}{180} \times 360^\circ$	10°
5 or more	2	$\frac{2}{180} \times 360^\circ$	4°
Total	180		

To find the angle:

$$\frac{\text{frequency}}{\text{total}} \times 360^\circ$$

5 or more

4 people

3 people

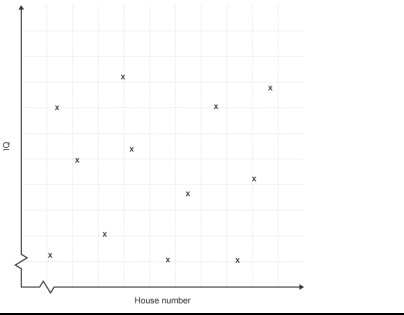
2 people

1 person

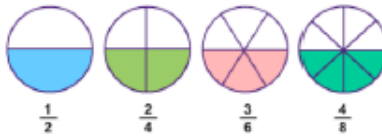
3d. SCATTER GRAPHS

13	Outliers		Outliers don't follow the trend
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14	Line of Best Fit	<p>A scatter plot with 'Rainfall (mm)' on the x-axis (0 to 7) and 'Umbrellas sold' on the y-axis (0 to 50). Data points are marked with 'x'. A solid purple line of best fit starts at (0,0) and passes through approximately (6.5, 38).</p>	<p>A sensible straight line that goes as centrally as possible through the points plotted.</p> <p>It should also follow the same steepness of the crosses.</p>	
15	Interpolate	<p>The same scatter plot as in row 14. A dashed red line is drawn from 3 on the x-axis, up to the line of best fit, and then across to the y-axis at approximately 18.</p>	<p>Using a line of best fit to estimate data <u>WITHIN</u> our range</p> <p><u>For example:</u> To estimate how many umbrellas are sold with 3mm rain.</p> <ul style="list-style-type: none"> <li>Find where 3 mm of rainfall is on the graph.</li> <li>Draw a line by going across from 3 mm and then down.</li> </ul>	
16	Extrapolate	<p>The same scatter plot as in row 14. The line of best fit is extended as a dotted purple line to 10 on the x-axis. A dashed red line is drawn from 10 on the x-axis, up to the dotted line, and then across to the y-axis at approximately 65.</p>	<p>Continuing a line of best fit to estimate data <u>BEYOND</u> our range (not as reliable as interpolation)</p> <p><u>For example:</u> To estimate how many umbrellas are sold with 10mm rain.</p> <ul style="list-style-type: none"> <li>Continue the line of best fit.</li> <li>Find where 10mm of rainfall is on the graph.</li> <li>Draw a line by going across from 10mm and then down.</li> </ul>	
17a	Positive Correlation	<p>A scatter plot with 'Temperature (°C)' on the x-axis (14 to 30) and 'Number of ice-creams sold' on the y-axis (50 to 102). Data points are marked with 'x' and show a clear upward trend.</p>	BOTH variables increase with each other	i.e. Ice creams sold vs Temperature
17b	Negative Correlation	<p>A scatter plot with 'Temperature (°C)' on the x-axis and 'Number of coats sold' on the y-axis. Data points are marked with 'x' and show a clear downward trend.</p>	ONE variable increases as the other decreases	i.e. Coats sold vs temperature

17c	No Correlation	 <p>A scatter plot on a grid. The vertical axis is labeled 'IQ' and the horizontal axis is labeled 'House number'. There are 12 data points represented by 'x' marks. The points are scattered randomly across the grid, showing no discernible pattern or trend, which indicates no correlation between the two variables.</p>	NO relationship between variables	i.e. IQ and House Number
18	Causation	<p>If one variable causes a change in the other.</p> <ul style="list-style-type: none"><li>• i.e. an increase temperature <u>WILL</u> cause an increase ice cream sales</li><li>• i.e. the number of bee stings <u>WILL NOT</u> cause an increase in ice cream sales (although both will increase in hot weather)</li></ul>		

## Fractions

1.	Fraction	Part of a whole	
2.	Numerator	The number on the top of the fraction	$\frac{\text{numerator}}{\text{denominator}}$
3.	Denominator	The number on the bottom of the fraction	
4.	Equivalent fractions	Fractions that have the same value but look different.	
5.	Improper fraction	A fraction where the numerator is larger than the denominator.	e.g. $\frac{4}{3}$
6.	Mixed number	A number made from integer and fraction parts.	e.g. $2\frac{2}{3}$
7.	Unit fraction	A fraction that has a numerator of 1	
8.	Reciprocal	The reciprocal of a number is 1 divided by the number.	e.g. the reciprocal of 3 is $\frac{1}{3}$
		Dividing by a number is the same as multiplying by its reciprocal	e.g. $\times$ by $\frac{1}{3}$ is the same as $\div$ by 3

## Fractions - processes

9.	Simplifying fractions	Divide the numerator and denominator by the HCF.	$\frac{24}{30} = \frac{4}{5}$
10.	Finding equivalent fractions	Multiply the numerator and denominator by the same number	$\frac{4}{8} \times 2 = \frac{8}{16}$
11.	Comparing fractions	Write them with a common denominator	
12.	Fraction of an amount	Amount divided by the denominator then multiplied by the numerator	e.g. $\frac{5}{7}$ of 42 $42 \div 7 \times 5 = 30$
13.	Multiply fractions	Multiply the numerators and multiply the denominators	$\frac{6}{7} \times \frac{4}{5} = \frac{6 \times 4}{7 \times 5} = \frac{24}{35}$
14.	Divide fractions	<ul style="list-style-type: none"> <li>Flip the second fraction (find the reciprocal).</li> <li>Change the divide to multiply.</li> <li>Multiply the fractions.</li> </ul>	$\frac{4}{7} \div \frac{5}{6} = \frac{4}{7} \times \frac{6}{5} = \frac{4 \times 6}{7 \times 5} = \frac{24}{35}$

15.	Add or subtract fractions	<ul style="list-style-type: none"> <li>Write as fractions with a common denominator.</li> <li>Add or subtract the numerators</li> </ul>	$\frac{2}{8} + \frac{1}{6} = \frac{6}{24} + \frac{4}{24} = \frac{10}{24} = \frac{5}{12}$
16.	Convert improper fractions to mixed numbers	<ul style="list-style-type: none"> <li>Divide the numerator by the denominator</li> <li>The answer gives the whole number part.</li> <li>The remainder becomes the numerator of the fraction part with the same denominator.</li> </ul>	$\frac{43}{6} = 7\frac{1}{6}$
17.	Convert mixed numbers to improper fractions	<ul style="list-style-type: none"> <li>Multiply the denominator by the whole number part.</li> <li>Add the numerator to this.</li> <li>Put the answer to this back over the denominator</li> </ul>	$7\frac{1}{6} = \frac{6 \times 7 + 1}{6} = \frac{43}{6}$

## Percentages

18.	Percentage	Means 'out of 100'	
19.	Multiplier	A decimal you multiply by to represent a percentage	
		To use a multiplier to find a percentage, divide your percentage by 100, then multiply the amount by this value.	
20.	Percentage increase	Calculate the percentage and add onto the original	
		Or use a multiplier	$amount \times \frac{100 + \% \text{ increase}}{100}$
21.	Percentage decrease	Calculate the percentage and subtract from the original	
		Or use a multiplier	$amount \times \frac{100 - \% \text{ increase}}{100}$
22.	Percentage change	$\frac{\text{Change}}{\text{Original}} \times 100$	
23.	Express one number as a percentage of another	$\frac{\text{Number 1}}{\text{Number 2}} \times 100$	
24.	Reverse percentage	Use when asked to find the priginal amount after a percentage increase or decrease.	
		<p>Original Value x Multiplier = New Value</p> <p>Original Value = <math>\frac{\text{New Value}}{\text{Multiplier}}</math></p>	
25.	Interest	A fee paid for borrowing money or money earnt through investing.	



26.	Simple interest	Interest that is calculated as a percentage of the original	$I = Prt$  I – Interest P – Original amount r – interest rate t – time								
27.	Compound interest	When interest is calculate on the original amount and any previous interest	$P\left(1 + \frac{R}{100}\right)^n$  P – Original amount R – Interest rate n – the number of interest periods (e.g. yrs)								
		OR  <i>Original × Multiplier<sup>time</sup></i>									
28.	Tax	A financial charge placed on sales or savings by the government e.g. VAT									
29.	Loss	Income minus all expenses, resulting in a negative value									
30.	Profit	Income minus all expenses, resulting in a positive value									
31.	Depreciation	A reduction in the value of a product over time									
32.	Annual	Means yearly									
33.	Per annum	Means per year									
34.	Salary	A fixed regular payment, often paid monthly									
FDP Conversions											
35.	Percentage to decimal	Divide by 100									
36.	Decimal to percentage	Multiply by 100									
37.	Fraction to percentage	Find an equivalent fraction with 100 as the denominator									
38.	Percentage to fraction	Write as a fraction over 100 then simplify									
39.	Fraction to decimal	Carry out division or convert to a percentage first									
40.	Decimal to fraction	Use place value to find the denominator and simplify or convert to a percentage first.									
Basics to memorise											
41.	Fraction	$\frac{1}{100}$	$\frac{1}{10}$	$\frac{1}{8}$	$\frac{1}{5}$	$\frac{1}{4}$	$\frac{1}{3}$	$\frac{1}{2}$	$\frac{2}{3}$	$\frac{3}{4}$	
	Decimal	0.01	0.1	0.125	0.2	0.25	0.3̇	0.5	0.6̇	0.75	
	Percentage	1%	10%	12.5%	20%	25%	33.3̇%	50%	66.7̇%	75%	

## Equations

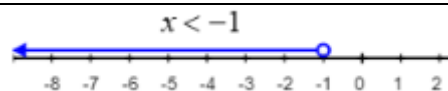
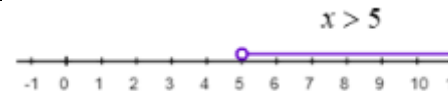
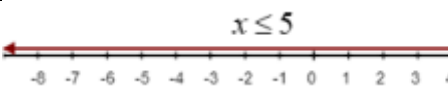

1.	Equation	Contains an 'equals' sign		e.g.	$3y - 3 = 12$
		Has at least one variable			
2.	Linear	Produces a straight line graph			
		No indices above 1			
3.	Term	One part of an expression/equation/formula		e.g.	$4c$ $\frac{w}{5}$
		Can involve multiplying and dividing coefficients and variables			
		Separated from other terms by addition and subtraction			
4.	Expression	One or a group of terms.		e.g.	$3y - 3$ $3y^2 + y^3$
		Can include variables, constants, operators and grouping symbols.			
		No 'equals' sign			
5.	Formula	A special type of equation that shows the relationship between a set of variables			
6.	Identity	An equation that is true no matter what values are chosen, $\equiv$		e.g.	$3y \equiv 2y - y$ for any value of $y$ .
7.	Unknown	A letter representing a number			
8.	Solve	TO find the value of the unknown			
9.	Inverse operations	The operation used to reverse the original operation			
		+ and - are inverse		$\times$ and $\div$ are inverse	
		Finding the square root is the inverse of finding the square of a number.			
		Finding the cube root is the inverse of finding the cube of a number.			



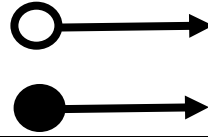
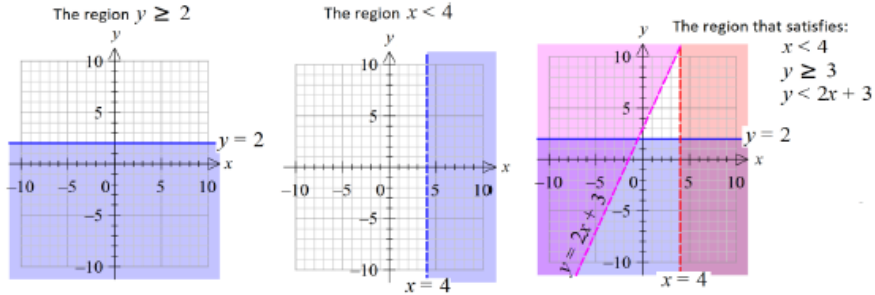
## Solving equations

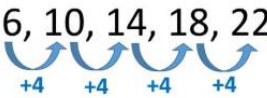
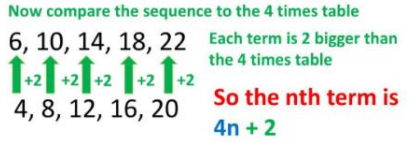
10.	To solve equations we need to use inverse operations														
11.	What ever you do to one side of the equals sign you must do the same to the other														
12.	One step	<table border="1"> <tr> <td><math>x + 4 = 7</math></td> <td><math>x - 5 = 12</math></td> <td><math>3x = 18</math></td> <td><math>\frac{x}{4} = 6</math></td> </tr> <tr> <td><math>(-4) \quad (-4)</math></td> <td><math>(+5) \quad (+5)</math></td> <td><math>(\div 3) \quad (\div 3)</math></td> <td><math>(\times 4) \quad (\times 4)</math></td> </tr> <tr> <td><math>x = 11</math></td> <td><math>x = 17</math></td> <td><math>x = 1</math></td> <td><math>x = 24</math></td> </tr> </table>		$x + 4 = 7$	$x - 5 = 12$	$3x = 18$	$\frac{x}{4} = 6$	$(-4) \quad (-4)$	$(+5) \quad (+5)$	$(\div 3) \quad (\div 3)$	$(\times 4) \quad (\times 4)$	$x = 11$	$x = 17$	$x = 1$	$x = 24$
$x + 4 = 7$	$x - 5 = 12$	$3x = 18$	$\frac{x}{4} = 6$												
$(-4) \quad (-4)$	$(+5) \quad (+5)$	$(\div 3) \quad (\div 3)$	$(\times 4) \quad (\times 4)$												
$x = 11$	$x = 17$	$x = 1$	$x = 24$												

13.	Two step	Requires the use of two inverse operations	$2x - 7 = 19$ $2x = 26$ $x = 13$
14.	With brackets	Expand the brackets first $5(2x + 1) = 35$ $10x + 5 = 35$ $10x = 30$ $x = 3$	OR if possible divide by the number outside of the bracket first $4(2x + 4) = 20$ $2x + 4 = 5$ $2x = 1$ $x = \frac{1}{2}$
15.	Unknowns on both sides	Start by eliminating the unknown from one of the signs.	$5x + 2 = 3x - 8$ $2x + 2 = -8$ $2x = -10$ $x = -5$
16.	With fractions	Eliminate any terms that are being added or subtracted separate from the fraction first. $\frac{f}{5} + 2 = 8$ $\frac{f}{5} = 6$ $f = 30$	If everything is part of the fraction then multiply by the denominator first. $\frac{f + 2}{5} = 8$ $f + 2 = 40$ $f = 38$

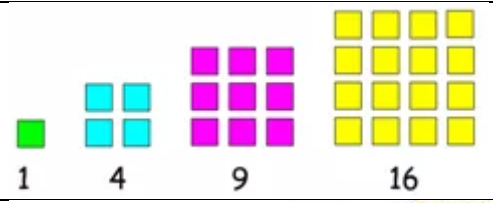
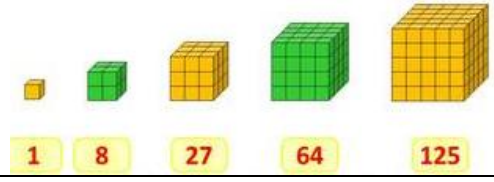
## Inequalities


17.	Inequality	The relationship between two expressions that are not equal	
18.	=	Equal to	
19.	≠	Not equal to	
20.	<	Less than	
21.	>	Greater than	
22.	≤	Less than or equal to	
23.	≥	Greater than or equal to	

24.	Inclusive	Gives a finites rnage of solutions	e.g. $3 < x \leq 8$
25.	Exclusive	Gives an infinite range of solutions	e.g. $x > 5$ $-4 \leq x$
26.	Integer	A whole number that can be positive negative or zero	
27.	Solve	Inequalities are solved in the same way as solving equations	
		Only exception: if you multiply or divide by a negative number you must swap the sign e.g. less than to greater than	
28.	List integers solutions	Give the integers that satisfy the inequality	
		e.g. $x > 6$ integer solutions are 6, 7, 8....	
		e.g. $-5 < x \leq 5$ integer solutions are -4, -3, -2, -1, 0, 1, 2, 3, 4, 5	
29.	Represent on a number line	An empty circle shows the value is not included	
		A shaded circle shows the value is included	
		An arrow shows that the solution continues to infinity	
30.	Inequalities on graphs	 <p>The unwanted sections are shaded</p>	
		Dashed lines are used to represent $<$ or $>$	
		Solid line is used to represent $\leq$ or $\geq$	
<b>Sequences</b>			
31.	Sequence	An order pattern of numbers or diagrams	
32.	Term	One of the numbers or diagrams in a sequence	
33.	Term to term rule	The rule for moving from one term to the next in a sequence	
34.	Formula	A rule written to describe a reallationship between twp quantities	
35.	Arithmetic sequence	A sequence where the term to term rule is to addd or subtract the same amount echg time	

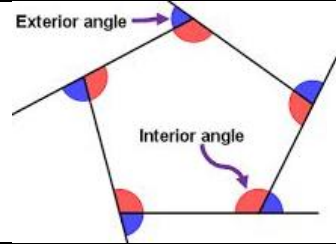

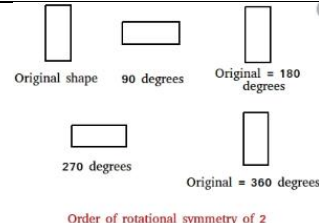
36.	Quadratic sequence	A sequence where the term to term rule is changing by the same amount each time
		The second difference is a constant amount.
37.	Geometric sequence	A sequence where the term to term rule is to multiply by the same amount each time
38.	Common ratio	The value a geometric sequence is multiplied by from one term to the next
		Denoted by the letter $r$
39.	Series	The sum of the terms in a sequence
40.	Position to term rule	The rule for finding any value of a sequence
41.	nth term rule for an arithmetic sequence	The rule to find any term in a sequence of numbers
		<ul style="list-style-type: none"> <li>Find the common difference between the terms</li> <li>This becomes your coefficient of <math>n</math> (this is the times table the sequence is linked to)</li> <li>The number you need to add or subtract to get to the second term becomes the second term in the nth term rule</li> </ul> <p>          6, 10, 14, 18, 22 The sequence increases by 4, so the nth term starts with <math>4n</math> </p> <p>          Now compare the sequence to the 4 times table          6, 10, 14, 18, 22 Each term is 2 bigger than the 4 times table          4, 8, 12, 16, 20 So the nth term is <math>4n + 2</math> </p>
42.	nth term for a geometric sequence	<ul style="list-style-type: none"> <li>Divide the second sequence by the first to find the common ratio, <math>r</math></li> <li>The nth term is <math>ar^{n-1}</math> where <math>a</math> is the first term and <math>n</math> is the term position in the sequence</li> </ul>
43.	Finite	Has a final point
44.	Infinite	Carries on forever
45.	Ascending	Increases
46.	Descending	Decreases
47.	Linear function	An arithmetic sequence that can be represented by a straight line graph

### Special Sequences








48.	Square numbers	1, 4, 9, 16, 25, 36, 49, 64, 81, 100	
49.	Cube numbers	1, 8, 27, 64, 125	

50.	Triangular numbers	1, 3, 6, 10, 15, 21, 28	
51.	Fibonacci sequence	A sequence where each term is the sum of the two previous terms e.g. 1, 1, 2, 3, 5, 8, 13, 21...	

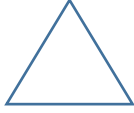

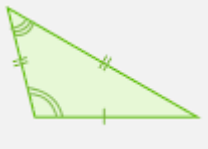
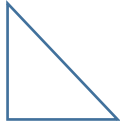
### Shapes and angles - definitions

1.	Angle	A measure of turn, measured in degrees °	
2.	Protractor	Instrument used to measure the size of an angle	
3.	Acute angle	An angle less than 90°	
4.	Right angle	A 90° angle	
5.	Obtuse angle	An angle more than 90° but less than 180°	
6.	Reflex angle	An angle more than 180°	
7.	Parallel lines	Lines that are equal distance apart that will never meet even when extended	
8.	Perpendicular lines	Lines that intersect at a right angle	
9.	Polygon	A 2D shape with straight lines only	
10.	Regular polygon	A polygon where:	
		All sides are the same length All angles are the same size	
11.	Interior angles (I)	An angle inside a polygon	
12.	Exterior angles (E)	An angle outside a polygon	
13.	Congruent	Shapes that are the same shapes and size, they are identical.	
14.	Similar	Shapes that are the same shape but are different sizes	
15.	Bisect	Cut in half	
16.	Tessellate	Fit together without leaving gaps	
17.	Symmetry	A shape has symmetry if a central line is drawn to show both sides are exactly the same.	
		We call these lines of symmetry	
18.	Rotational symmetry	A shape has rotational symmetry when it looks the same after some rotation of less than a full turn	


### Quadrilaterals (4 sided shapes)

19.	Square		4 equal sides 4 equal angles 2 pairs of parallel sides Diagonals cross at right angles	4 lines symmetry Rotational symmetry order 4
20.	Rectangle		2 pairs of equal sides 4 right angles 3 pairs of parallel sides	2 lines of symmetry Rotational symmetry order 2
21.	Rhombus		4 equal sides 2 pairs of equal angles 2 pairs of parallel sides Diagonals cross at right angles	2 lines of symmetry Rotational symmetry order 2
22.	Parallelogram		2 pairs of equal sides 2 pairs of equal angles 2 pairs of parallel sides	0 lines of symmetry Rotational symmetry order 2
23.	Kite		2 pairs of equal sides 1 pair of equal angles 2 pairs of parallel sides Diagonals cross at right angles	1 line of symmetry Rotational symmetry order 1
24.	Trapezium		One pair of parallel lines	
25.	Isosceles trapezium		1 pair of parallel sides 1 pair of equal sides 2 pairs of equal angles	1 line of symmetry Rotational symmetry order 1

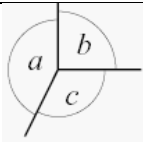
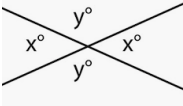
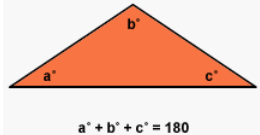
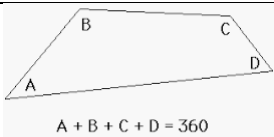
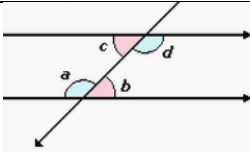
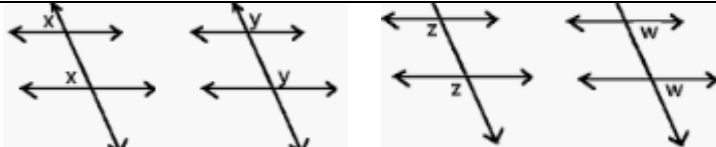
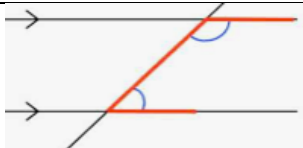
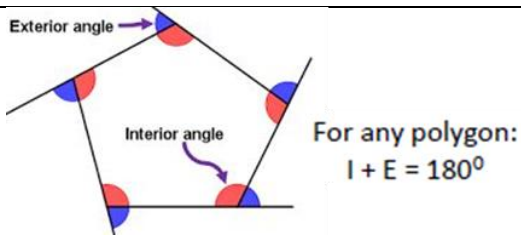
### Triangles (3 sided shapes)

26.	Equilateral		3 equal sides 3 equal angles	3 lines of symmetry Rotational symmetry order 3
27.	Isosceles		2 equal sides 2 equal angles	1 line of symmetry Rotational symmetry order 1
28.	Scalene		No equal sides No equal angles	
29.	Right-angled		1 right angle Can be scalene or isosceles	

### Basic angle rules

30.	Angles on a straight line add to $180^\circ$	
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31.	Angles around a point add up to $360^\circ$	
32.	Vertically opposite angles are equal	
33.	Angles in a triangle add to $180^\circ$	
34.	Angles in a quadrilateral add up to $360^\circ$	
<b>Angles on parallel lines</b>		
35.	Alternate angles are equal	
36.	Corresponding angles are equal	
37.	Co-interior angles add up to $180^\circ$	
<b>Angles in polygons</b>		
38.	Interior and exterior angles add to give $180^\circ$	
39.	Sum of interior angles	<p>For a 'n' sided polygon</p> <p>Sum of interior angles = <math>180 \times (n-2)</math></p>

40.	Size of one interior angle	For a 'n' sided polygon Interior angle = $\frac{180 \times (n-2)}{n}$
41.	Sum of exterior angles	For all polygons, sum of exterior angles = 360°
42.	Regular polygons	Exterior angle = 360 ÷ number of sides
		Number of sides = 360 ÷ exterior angle
		Interior angle = 180 – exterior angle

## Statistics and sampling: definitions

1.	Primary	Data that is collector by the researcher first hand			
2.	Secondary	Data that is collected by someone other than the user			
3.	Qualitative	Data described by words		e.g. favourite colour	
4.	Quantitative	Data that is categorised by numbers, can be discrete or continuous		e.g. height, shoe size	
5.	Discrete	Can be counted, can only have a finite number of possible values		e.g. number of people in a class	
6.	Continuous	Can be measured, can have an infinite number of possible values within a given range		e.g. height, weight, time, distance	
7.	Population	The whole group			
8.	Census	A survey of the whole population			
9.	Sample	A selection of the whole population			
10.	Survey	A tool used to gather information from individuals			
11.	Bias	Prejudice or favour shown for one person, group, thing or opinion over another.		e.g. asking people leaving a library whether they enjoyed reading	
12.	Random sample	Every member of the population has an equal chance of being selected.			
13.	Inequality signs	< less than	> greater than	≤ less than or equal to	≥ greater than or equal to
14.	Frequency	How often something occurs			
15.	Estimate	Find a value close to the correct answer if you were to calculate accurately			
16.	Interval	What is between two values of points		e.g. all the numbers between 0 and 10	
17.	Midpoint	The middle or half way point of an interval		e.g. the midpoint of all the umbers between 0 and 10 is 5	

## Measures of central tendency and spread

18.	Central tendency	A calculated central value of a set of numbers	Mean, median and mode are measures of central tendency
19.	Spread	Describes how similar or varied a set of values are	Range and interquartile range are measures of spread

20.	Mean	Add up all the mounts then divide by how many there are.
21.	Median	Put values in order and locate the middle value
22.	Mode	The value that occurs most often i.e. has the highest frequency.
23.	Range	The biggest value minus the smaller value
24.	Outlier	An extreme data value that doesn't fit with the overall trend or pattern

### Advantages and disadvantages of averages

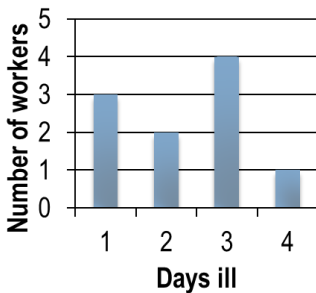
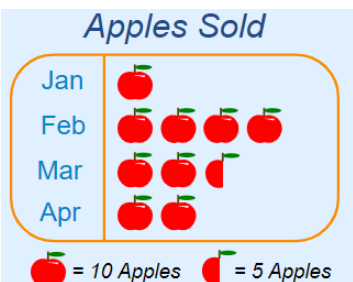


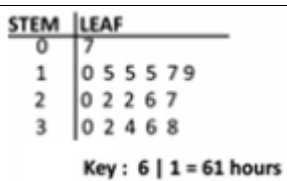
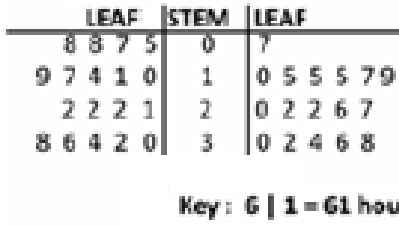
	Average	Advantages	Disadvantages
26.	Mean	Every value is included	Affected by extreme values
	Median	Not affected by extreme values	May not change if a data value changes
	Mode	Easy to find; not affected by extreme values; can be used with non-numerical data	There may not be a mode

### Averages from frequency tables

27.	Modal class	The class with the highest frequency
28.	Median	If the total frequency is $n$ , then the median lies in the class with the $\frac{n+1}{2}$ th value in it.

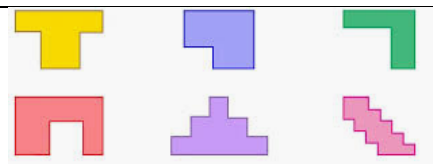
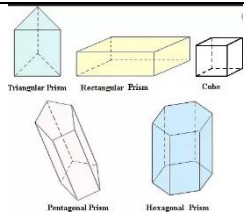
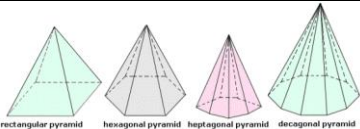
29.	<p>Mean from a frequency table</p> <p>Times → Add ↓↓ Divide ←</p>	<p>No of make-up items in handbags</p> <table border="1"> <thead> <tr> <th>No of Items <math>x</math></th><th>Freq <math>f</math></th><th><math>f \times x</math></th></tr> </thead> <tbody> <tr> <td>1</td><td>7</td><td><math>1 \times 7 = 7</math></td></tr> <tr> <td>2</td><td>2</td><td><math>2 \times 2 = 4</math></td></tr> <tr> <td>3</td><td>1</td><td><math>3 \times 1 = 3</math></td></tr> <tr> <td>4</td><td>4</td><td><math>4 \times 4 = 16</math></td></tr> <tr> <td>5</td><td>2</td><td><math>5 \times 2 = 10</math></td></tr> <tr> <td></td><td>16</td><td>40</td></tr> </tbody> </table> <p>Mean = <math>\frac{40}{16} = 2.5</math></p>	No of Items $x$	Freq $f$	$f \times x$	1	7	$1 \times 7 = 7$	2	2	$2 \times 2 = 4$	3	1	$3 \times 1 = 3$	4	4	$4 \times 4 = 16$	5	2	$5 \times 2 = 10$		16	40
No of Items $x$	Freq $f$	$f \times x$																					
1	7	$1 \times 7 = 7$																					
2	2	$2 \times 2 = 4$																					
3	1	$3 \times 1 = 3$																					
4	4	$4 \times 4 = 16$																					
5	2	$5 \times 2 = 10$																					
	16	40																					

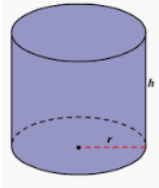
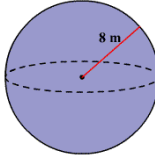
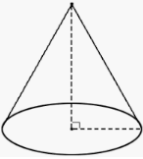
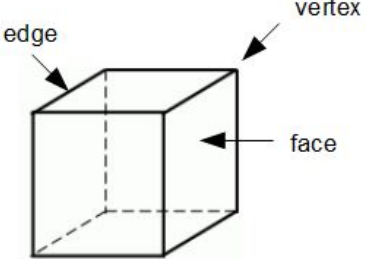
30.	Estimated mean from a grouped frequency table																								
	<div>Times →</div> <div>Add ↓↓</div> <div>Divide ←</div>	<table><tr><th>Class Interval</th><th>Mid-point</th><th>Frequency</th><th>Mid-point × Frequency</th></tr><tr><td><math>140 \leq h &lt; 150</math></td><td>145</td><td>6</td><td><math>145 \times 6 = 870</math></td></tr><tr><td><math>150 \leq h &lt; 160</math></td><td>155</td><td>16</td><td><math>155 \times 16 = 2480</math></td></tr><tr><td><math>160 \leq h &lt; 170</math></td><td>165</td><td>21</td><td><math>165 \times 21 = 3465</math></td></tr><tr><td><math>170 \leq h &lt; 180</math></td><td>175</td><td>8</td><td><math>175 \times 8 = 1400</math></td></tr><tr><td></td><td>Totals</td><td>51</td><td>8215</td></tr></table> <div>Mean = <math>8215 \div 51</math> =161.07843... = 161.08 (2dp)</div>	Class Interval	Mid-point	Frequency	Mid-point × Frequency	$140 \leq h < 150$	145	6	$145 \times 6 = 870$	$150 \leq h < 160$	155	16	$155 \times 16 = 2480$	$160 \leq h < 170$	165	21	$165 \times 21 = 3465$	$170 \leq h < 180$	175	8	$175 \times 8 = 1400$		Totals	51
Class Interval	Mid-point	Frequency	Mid-point × Frequency																						
$140 \leq h < 150$	145	6	$145 \times 6 = 870$																						
$150 \leq h < 160$	155	16	$155 \times 16 = 2480$																						
$160 \leq h < 170$	165	21	$165 \times 21 = 3465$																						
$170 \leq h < 180$	175	8	$175 \times 8 = 1400$																						
	Totals	51	8215																						

31.	Estimate of range from grouped frequency table	The maximum possible value minus the smallest possible value.	
Averages from charts/graphs			
32.	Bar chart	<p>A chart to display discrete data where the height of the bar shows the frequency.</p> <p style="text-align: center;"><b>Worker absences</b></p>  <p>Number of workers</p> <p>Days ill</p>	<p>Mean: <math>23 \div 10 = 2.3</math> Median: 2.5 Mode : 3 Range: <math>4-1 = 3</math></p>
33.	Pictogram	<p>A chart that uses pictures to represent quantities. Must include a key.</p> <p style="text-align: center;"><i>Apples Sold</i></p>  <p>Jan Feb Mar Apr</p> <p> = 10 Apples     = 5 Apples</p>	<p>Mean: <math>95 \div 4 = 23.75</math> Median: 22.5 Range: 30</p>
34.	Stem and leaf diagram	 <p>Key : 6   1 = 61 hours</p> <p>A diagram that shows groups of data arranged by place value. 'Leaves' should be in order. Must have a key.</p>	<p>Mean: <math>385 \div 17 = 22.6</math> Median: 22 Mode: 15 Range: <math>38-7 = 31</math></p>
35.	Back to back stem and leaf	<p>Compares two sets of results. Must have a key.</p> <p style="text-align: center;"><b>A</b>                      <b>B</b></p>  <p>Key : 6   1 = 61 hours</p>	<p>Set A Mean: <math>356 \div 18 = 19.8</math> Median: 20 Mode: 22 Range: <math>38-5 = 33</math></p> <p>Set B Mean: <math>385 \div 17 = 22.6</math> Median: 22 Mode: 15 Range: <math>38-7 = 31</math></p>

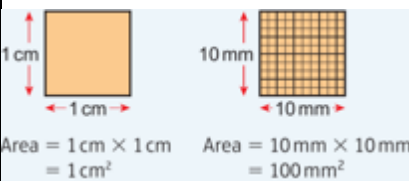


## 2D and 3D shapes: definitions

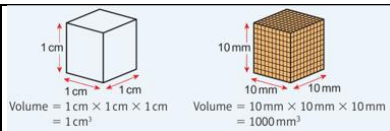
1.	Dimension	The size of something in a particular direction e.g. height, depth, length, width	
2.	2D shape	A shape that has length/height and a width but no depth	
3.	3D shape	A shape that depth as well as length/height and width	
4.	Polygon	A 2D shape with straight lines only	
5.	Regular polygon	A polygon where:	
		All sides are the same length All angles are the same size	
6.	Compound shape	A shape made up of two or more simple shapes	
7.	Rectilinear shape	A shape where all of its sides meet at right angles	
8.	Perimeter	The distance around the outside of a 2D shape	
9.	Area	The space inside a 2D shape	
10.	Surface area	The total area of all the faces of a 3D shape	
11.	Volume	The space inside a 3D shape	
12.	Capacity	The amount of fluid a 3D object can hold	
13.	S.I. Units	Standard units of measurement used by scientists across the world	
14.	Metric units	Standard units of measurement that vary by powers of 10	
15.	Imperial units	Older units of measurement, some of which are still common e.g. miles, gallons	
16.	Cross section	The shape we get when cutting straight through a 3D shape	
17.	Prism	A 3D shape that has a constant cross section through its length	
18.	Pyramid	A 3D shape with a polygon as its base and triangular sides that meet at the top	

19.	Cylinder	A prism with two circular ends connected by a curved surface	
20.	Sphere	A 3D shape where all points on the surface are the same distance from the centre	
21.	Spherical	Means in the shape of a sphere	
22.	Cone	A 2D shape that has a circular base joined to a point by a curved side	
23.	Face	A flat surface of a 3D shape (can be curved)	
24.	Edge	A line segment where two faces meet	
25.	Vertex	A point where two or more edges meet	
26.	Vertices	Plural of vertex	

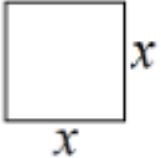
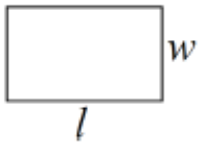
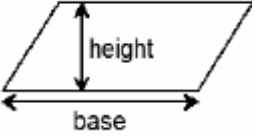
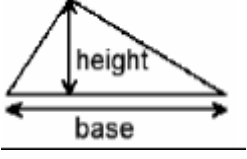
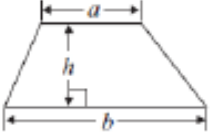
## Measures

27.	Units of time	Standard units of time are seconds, minutes, hours, days, years			
		60 seconds = 1 minute	60 minutes = 1 hour	24 hours = 1 day	365 days = 1 year
28.	Units of mass	Metric units of mass are milligrams, grams, kilograms and tonnes			
		1000mg = 1g	1000g = 1kg	1000kg = 1 tonne	
29.	Units of length	Metric units of length are millimetres, centimetres, metres and kilometres			
		10mm = 1cm	100cm = 1m	1000m = 1km	
30.	Units of area	Metric units of length are millimetres <sup>2</sup> , centimetres <sup>2</sup> , metres <sup>2</sup> and kilometres <sup>2</sup>			
		1cm <sup>2</sup> = 100mm <sup>2</sup>			
		1m <sup>2</sup> = 1000cm <sup>2</sup>			



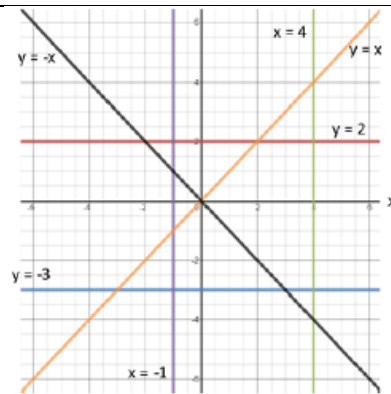
31.	Units of volume	Metric units of length are millimetres <sup>3</sup> , centimetres <sup>3</sup> , metres <sup>3</sup> and kilometres <sup>3</sup>	
		1cm <sup>3</sup> = 1000mm <sup>3</sup>	
		1m <sup>3</sup> = 1000000cm <sup>3</sup>	
32.	Units of capacity	Metric units of capacity are millilitres, centilitres and litres	
		10ml = 1cl	1000ml = 100cl = 1l
33.	Capacity and volume conversions	1cm <sup>3</sup> = 1ml	1000cm <sup>3</sup> = 1l

## 2D Shapes

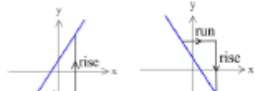
34.	Square	Area = $l \times w$ or $l^2$ as length and width are equal	
35.		Perimeter = $l + l + l + l$ or $4l$	
36.	Rectangle	Area = $l \times w$	
37.		Perimeter = $l + l + w + w$ or $2l + 2w$	
38.	Parallelogram	Area = $b \times h$	
39.	Triangle	Area = $\frac{b \times h}{2}$ or $\frac{1}{2} \times b \times h$	
40.	Trapezium	Area = $\frac{a+b}{2} \times h$ or $\frac{1}{2} (a + b) \times h$	

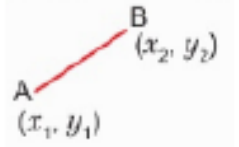
41.	Compound shape	<p>To find the area, split up into simple shapes, find each area and add together.</p> <p>To find the perimeter, find any missing sides then add all the sides together.</p>	
<b>3D shapes: volume</b>			
42.	Prism	<p><b>Volume</b> = <i>area of cross section</i> × <i>length</i></p>	
43.	Cuboid	<p><b>Volume</b> = <i>area of cross section</i> × <i>length</i></p> <p><b>Volume</b> = <i>length</i> × <i>width</i> × <i>height</i></p>	
44.	Triangular prism	<p><b>Volume</b> = <i>area of cross section</i> × <i>length</i></p> <p><b>Volume</b> = <math>\frac{1}{2} \times \text{base} \times \text{height} \times \text{length}</math></p>	

### Graphs - definitions

1.	Axis	A reference line on a graph		
2.	Axes	Plural of axis		
3.	Quadrant	A quarter of a graph separated by a axes		
4.	Coordinate	Used to show a position on a coordinate plane, $(x, y)$		
		First coordinate is the horizontal position, (x axis) and the second is the vertical position (y axis)		
5.	Origin	The point $(0,0)$ on a set of axes		
6.	Plot	Mark a position or positions on a graph		
7.	y intercept	The y value where a graph crosses the y axis	where $x=0$	
8.	x intercept	The x value where a graph crosses the x axis	where $y=0$	
9.	Parallel	Lines that are equal distance apart that if extended will never meet		
10.	"y=" graph	Constant y coordinate		
		Will be parallel to the x axis		
11.	"x=" graph	Constant x coordinate		
		Will be parallel to the y axis		
12.	Linear function	An arithmetic sequence that can be represented by a straight line graph		
13.	Linear equation	An equation that produces a straight line graph		
14.	$y = mx = c$	The general equation of a straight line	$m = \text{gradient}$ and $c = \text{y intercept}$	

### Linear graphs

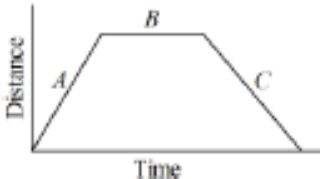
15.	Gradient	The steepness of a graph	 <p>This has a positive gradient      This has a negative gradient</p>
		$\text{Gradient} = \frac{\text{change in } y}{\text{change in } x}$ $= \frac{\text{rise}}{\text{run}}$	

16.	Gradient between two points	<p>If <math>A = (x_1, y_1)</math> and <math>B = (x_2, y_2)</math></p> <p>The gradient of line AB = <math>\frac{y_2 - y_1}{x_2 - x_1}</math></p>	
17.	Parallel lines	Have the same gradients	
18.	Mid-point	The coordinate half way between two point	<p>If <math>A = (x_1, y_1)</math> and <math>B = (x_2, y_2)</math></p> <p>the mid-point is <math>\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)</math></p>

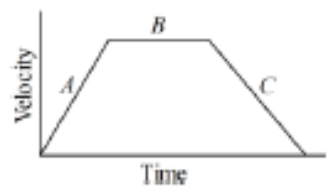
### Real life graphs

19.	Steady speed	Travelling the same distance each minute
20.	Velocity	Speed in a particular direction
21.	Rate of change	Shows how a variable changes over time
22.	Acceleration	How fast velocity changes; measured in $m/s^2$ or $km/s^2$ etc

### Distance - Time graphs

23.	Represent a journey	 <p>A = steady speed, B = no movement, C = steady speed back to start</p>
24.	Vertical axis represents the distance from the starting point	
25.	Horizontal axis represents the time taken	
26.	Straight lines mean constant speed	
27.	Horizontal lines mean no movement	
28.	Gradient = speed	
29.	$\text{Average speed} = \frac{\text{total distance}}{\text{total time}}$	

### Velocity – Time graphs

30.	Represents the speed at given times	 <p>A = steady acceleration, B = constant speed, C = steady deceleration back to a stop</p>
31.	Straight lines mean constant acceleration or deceleration	
32.	Horizontal change means no change in velocity e.g. constant speed	
33.	Positive gradient = acceleration	
34.	Negative gradient = deceleration	
35.	Distance travelled = area under the graph	

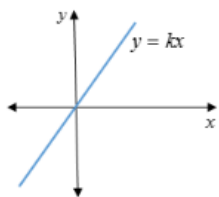
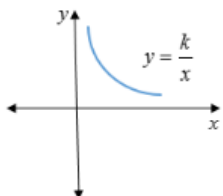


## Transformations - definitions


1.	Transformation	Changing a 2D shape in some way.			
		Rotation	Reflection	Translation	Enlargement
2.	Object	The name given to a shape before a transformation has occurred.			
3.	Image	The name given to a shape after a transformation has occurred			
4.	Rotation	A circular movement about a fixed point			
5.	Centre of rotation	The fixed point that the shape has been rotated about			
		Written as a coordinate $(x, y)$			
6.	Direction	Clockwise or anticlockwise			
7.	Reflection	An image as it would be seen in a mirror			
8.	Line of reflection	The “mirror line” used to perform reflections.			
		Written using algebraic notation e.g. $y = 3$ , $x = -2$ , $y = x$ or x/y axis			
9.	Translation	The movement of a shape without rotating or flipping it			
10.	Column vector	Notation used to represent translations		$\begin{pmatrix} x \\ - \\ y \end{pmatrix}$	
		x is the horizontal movement			
		y is the vertical movement			
11.	Resultant vector	The vector that moves the shape to its final position after more than one translation			
12.	Enlargement	A change in size of a shape (can be bigger or smaller)			
13.	Scale factor	The proportions by which the dimensions of an object will increase/decrease by			
		If fractional then the image will be smaller than the object			
14.	Centre of enlargement	A fixed point to enlarge an object from			
		Written as a coordinate $(x, y)$			
15.	Single transformation	Where the object is only transformed once			
16.	Combination	Where the object is transformed multiple times			
17..	Origin	The point (0,0); where the x and y axis intersect			
18.	Similar	Same shape but different sizes			
		e.g. similar shapes are enlargements of one another			

19.	Congruent	Shapes that are the same shape and size	
20.	Describe	Use key words to accurately state what has happened to an object to make the resulting image	
Transformations			
21.	Rotation	<p>To carry out you need to:</p> <ol style="list-style-type: none"><li>1. Draw object on tracing paper</li><li>2. Place pencil on 'centre of rotation' and carry out the motion</li><li>3. Draw your image on the grid</li></ol>	<p>To describe you need to write:</p> <ol style="list-style-type: none"><li>a) "rotation"</li><li>b) angle of rotation</li><li>c) direction of rotation</li><li>d) centre of rotation</li></ol>
22.	Reflection	<p>To carry out you need to:</p> <ol style="list-style-type: none"><li>1. If required draw the 'line of reflection'</li><li>2. Count squares from object to line and repeat the other side of the line for all corners of the object</li><li>3. Join points up to create the image</li></ol>	<p>To describe you need to write:</p> <ol style="list-style-type: none"><li>a) "reflection"</li><li>b) the equation of the line of reflection</li></ol>
23.	Translation	<p>To carry out you need to:</p> <ol style="list-style-type: none"><li>1. Use vector notation to work out the horizontal and vertical movement</li><li>2. Count squares to carry out movement on all corners of the object</li><li>3. Join up points to create the image</li></ol>	<p>To describe you need to write:</p> <ol style="list-style-type: none"><li>a) "translation"</li><li>b) the column vector</li></ol>
24.	Enlargement	<p>To carry out you need to:</p> <ol style="list-style-type: none"><li>1. If required cross the coordinate that is the centre of enlargement</li><li>2. For each corner count from the line of reflection to the object</li><li>3. Multiply this movement by the required scale factor</li><li>4. Draw new corners from the centre of enlargement with new horizontal and vertical movement</li><li>5. Join up points to create image</li></ol>	<p>To describe you need to write:</p> <ol style="list-style-type: none"><li>a) "enlargement"</li><li>b) the scale factor</li><li>c) the centre of enlargement</li></ol>

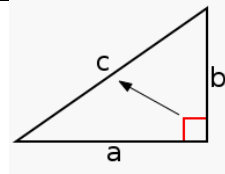
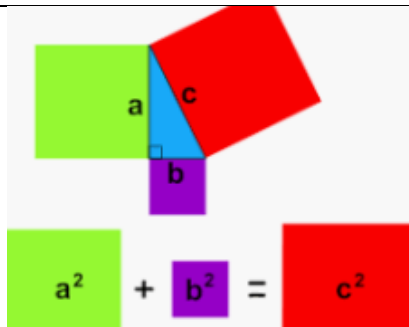
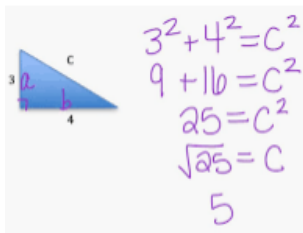
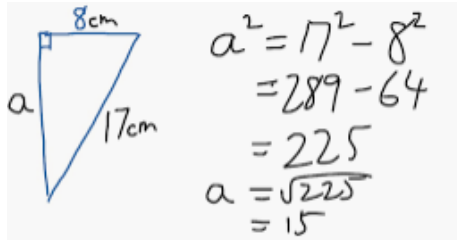
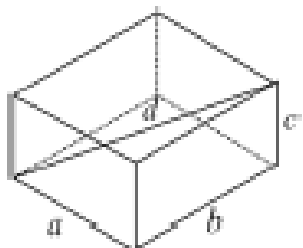
## Ratio and Proportion - definitions

1.	Ratio	A relationship between two or more quantities	
2.	Unit ratio	Used to compare ratios, one of the parts is 1	
		The only time it is permissible to have a decimal in a ratio	
3.	Equivalent	Ratios that have the same simplified form are said to be equivalent	
4.	Scale	A ratio that represents the relationship between a length on a drawing or a map and the actual length	
5.	Proportion	Compares a part with a whole	
6.	Direct proportion	Two quantities increase at the same rate	$y \propto x$ $y = kx \text{ for a constant } k$ 
		Graph is a straight line that goes through the origin	
7.	Inverse/indirect proportion	One variable increases at a constant rate as the second variable decreases	$y \propto \frac{1}{x}$ $y = \frac{k}{x} \text{ for a constant } k$ 
8.	Proportional	A change in one is always accompanied by a change in the other	
9.	Constant of proportionality	Represented by $k$	
		Its value stays the same	
10.	Share	Splitting into parts as defined by a ratio	
11.	Unitary method	Finding the value of 1 item then using this to find the value of any number of that item	

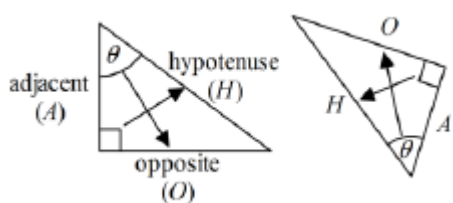
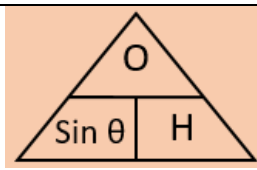
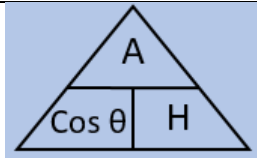
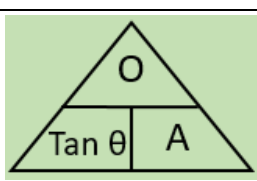
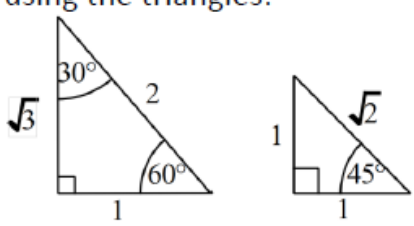
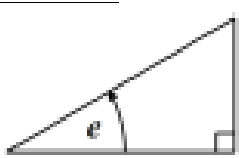
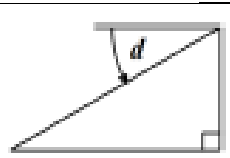


		Use to work out which products give the best value for money	
Working with ratios			
12.	Simplifying ratio	Divide all parts by the highest common factor	e.g. 12:4 simplifies to 3:1 (divided by HCF of 4)
		All parts in the simplified version must be integers	
13.	Divide in a given ratio	Divide an amount so the ratio of the final values simplifies to the given ratio	<p>share £20 in the ratio 3 : 2</p> <p style="text-align: center;">£20</p> 

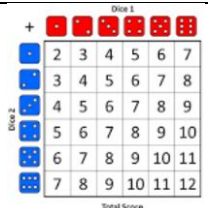
## Pythagoras' Theorem

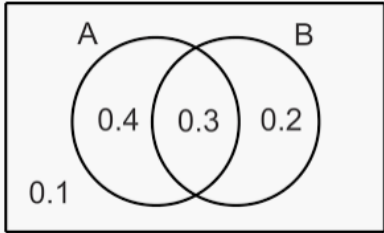
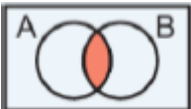
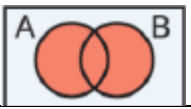
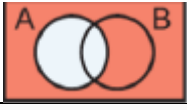

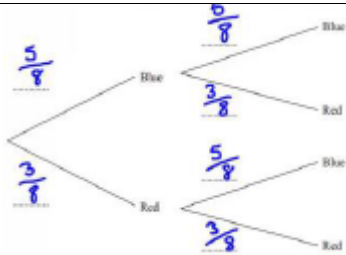
1.	Hypotenuse	The longest side of a right-angled triangle	
		It is always opposite the right angle	
2.	Right- angled triangle	A triangle that contains a right angle	
3.	Pythagoras' Theorem	$a^2 + b^2 = c^2$	
		Where c is the hypotenuse	
		Where a and b are the two shorter sides	
4.	To find the hypotenuse (c)		<ul style="list-style-type: none"><li>• Square</li><li>• Add</li><li>• Square root</li></ul>
5.	To find a short side (a/b)		<ul style="list-style-type: none"><li>• Square</li><li>• Subtract</li><li>• Square root</li></ul>
6.	Pythagoras' in 3D	$a^2 + b^2 + c^2 = d^2$	
		$d^2 - b^2 - c^2 = a^2$	

# Trigonometry - Right angled – SOH CAH TOA

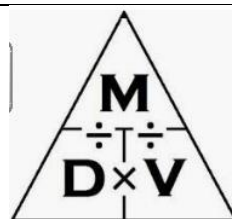
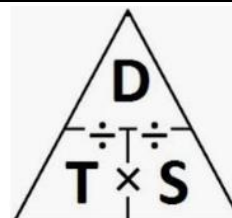

7.	Trigonometry	The ratios between the sides and angles of triangles																													
8.	Labelling the triangle	$\theta$ is the angle involved																													
		H is the hypotenuse																													
		O is the opposite																													
		A is the adjacent																													
9.	Sine	SOH				$\sin \theta = \frac{Opp}{Hyp}$																									
						$\theta = \sin^{-1} \frac{Opp}{Hyp}$																									
10.	Cosine	CAH				$\cos \theta = \frac{Adj}{Hyp}$																									
						$\theta = \cos^{-1} \frac{Adj}{Hyp}$																									
11.	Tangent	TOA				$\tan \theta = \frac{Opp}{Adj}$																									
						$\theta = \tan^{-1} \frac{Opp}{Adj}$																									
12.	Exact Values	<table><tr><td><math>\theta</math></td><td><math>0^\circ</math></td><td><math>30^\circ</math></td><td><math>45^\circ</math></td><td><math>60^\circ</math></td><td><math>90^\circ</math></td></tr><tr><td><math>\sin \theta</math></td><td>0</td><td><math>\frac{1}{2}</math></td><td><math>\frac{\sqrt{2}}{2}</math></td><td><math>\frac{\sqrt{3}}{2}</math></td><td>1</td></tr><tr><td><math>\cos \theta</math></td><td>1</td><td><math>\frac{\sqrt{3}}{2}</math></td><td><math>\frac{\sqrt{2}}{2}</math></td><td><math>\frac{1}{2}</math></td><td>0</td></tr><tr><td><math>\tan \theta</math></td><td>0</td><td><math>\frac{\sqrt{3}}{3}</math></td><td>1</td><td><math>\sqrt{3}</math></td><td></td></tr></table>						$\theta$	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$	$\sin \theta$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1	$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0	$\tan \theta$	0	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$	
		$\theta$	$0^\circ$	$30^\circ$	$45^\circ$	$60^\circ$	$90^\circ$																								
		$\sin \theta$	0	$\frac{1}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{3}}{2}$	1																								
		$\cos \theta$	1	$\frac{\sqrt{3}}{2}$	$\frac{\sqrt{2}}{2}$	$\frac{1}{2}$	0																								
		$\tan \theta$	0	$\frac{\sqrt{3}}{3}$	1	$\sqrt{3}$																									
These can be found using the triangles:																															
																															
13.	Angle of elevation		Angle of depression																												

## Probability - definitions

1.	Probability	<p>The extent to which an event is likely to occur</p> <p>Written as a fraction, decimal or percentage</p>	<p>For equally likely outcomes the probability that an event will happen is</p> $P = \frac{\text{number of successful outcomes}}{\text{total number of possible outcomes}}$
2.	Theoretical probability	Calculated without doing an experiment	
3.	Experimental probability	<p>Probabilities based on the data collected during an experiment</p> <p>Also known as estimated probability</p> <p>The more trials you do the more reliable your set of results</p>	$\text{estimated probability} = \frac{\text{frequency of event}}{\text{total frequency}}$
4.	P( ) notation	P( ) means the probability of the thing inside the brackets happening e.g. P(tails)	
5.	Experiment	A repeatable process that gives rise to a number of outcomes	
6.	Relative frequency	In an experiment, how often something happens as a proportion of the number of trials	$\text{Relative frequency} = \frac{\text{how often something happens}}{\text{all outcomes}}$
7.	Predictions	<p>You can predict the number of outcomes you will get using relative frequency</p> <p>Predicted number of outcomes = probability x number of trials</p>	
8.	Event	A collection of one or more outcomes	
9.	Independent	When one event has no effect on another	Here $P(A \text{ and } B) = P(A) \times P(B)$
10.	Dependent	When the outcome of one event, changes the probability of the next event	
11.	Exhaustive	Events are exhaustive if they cover all possible outcomes	
12.	Biased	Unfair	
13.	Unbiased	Fair	
14.	Sample space	The set of all possible outcomes	
15.	Sample space diagram	A diagram showing all possible outcomes from an experiment	

16.	Venn diagram	Can be used to represent events graphically		
		Frequencies or probabilities can be placed in the regions		
17.	$A \cap B$	A intersection B	All elements in A and B	
18.	$A \cup B$	A union B	All the elements in A OR B OR both	
19.	$A'$	Complement of A	Not in A	
20.	Mutually exclusive	Events that have no outcomes in common		 $P(A \text{ or } B) = P(A) + P(B)$
		Here $P(A \text{ or } B) = P(A) + P(B)$		
21.	Tree diagram	Used to show the outcomes of two (or more) events happening in succession		
22.	AND rule	Multiply the probabilities		
23.	OR rule	Add the probabilities		
24.	Conditional probability	The probability of a dependent event		
		The probability of a second outcome depends on what has already happened in the first outcome		

## Multiplicative reasoning – definitions and formulae

1.	Proportion	Compares a part with a whole	
2.	Proportional	A change in one is always accompanied by a change in another	
3.	Ratio	A relationship between two or more quantities	
4.	Compound measure	Combine measures of two different quantities	
5.	Density	The mass of a substance contained in a certain volume	
		Usually measured in g/cm³ or kg/m³	
		$density = \frac{mass}{volume}$	
6.	Velocity	Speed in a given direction	Usually measured in m/s
7.	Acceleration	The rate of change of velocity	Usually measured in m/s²
8.	Speed	The distance travelled in an amount of time	
		Usually measured in m/s, mph or km/h	
		$speed = \frac{distance}{time}$	
9.	Pressure	The force applied over an area	
		$pressure = \frac{force}{area}$	
		Usually measured in N/m²	

## Percentages

10.	Percentage	Means 'out of 100'
11.	Multiplier	A decimal you multiply by to represent a percentage
		To use a multiplier to find a percentage, divide your percentage by 100, then multiply the amount by this value.

12.	Percentage increase	Calculate the percentage and add onto the original	
		Or use a multiplier	$amount \times \frac{100 + \% \text{ increase}}{100}$
13.	Percentage decrease	Calculate the percentage and subtract from the original	
		Or use a multiplier	$amount \times \frac{100 - \% \text{ increase}}{100}$
14.	Percentage change	$\frac{\text{Change}}{\text{Original}} \times 100$	
15.	Express one number as a percentage of another	$\frac{\text{Number 1}}{\text{Number 2}} \times 100$	
16.	Reverse percentage	Use when asked to find the original amount after a percentage increase or decrease.	
		$\text{Original Value} \times \text{Multiplier} = \text{New Value}$ $\text{Original Value} = \frac{\text{New Value}}{\text{Multiplier}}$	
17.	Interest	A fee paid for borrowing money or money earned through investing.	
18.	Simple interest	Interest that is calculated as a percentage of the original	$I = Prt$ <p>           I – Interest            P – Original amount            r – interest rate            t – time         </p>
19.	Compound interest	When interest is calculate on the original amount and any previous interest	$P \left( 1 + \frac{R}{100} \right)^n$ <p>           P – Original amount            R – Interest rate            n – the number of interest periods (e.g. yrs)         </p>
		Or $\text{Original} \times \text{Multiplier}^{\text{time}}$	
20.	Tax	A financial charge placed on sales or savings by the government e.g. VAT	
21.	Loss	Income minus all expenses, resulting in a negative value	
22.	Profit	Income minus all expenses, resulting in a positive value	
23.	Depreciation	A reduction in the value of a product over time	

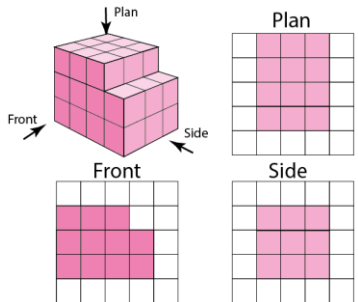
24.	Annual	Means yearly
25.	Per annum	Means per year
26.	Salary	A fixed regular payment, often paid monthly




## 2D shapes and 3D solids - definitions

1.	Face	A flat surface of a 3D shape
2.	Edge	A line segment where two faces meet
3.	Vertex	A point where two or more edges meet
4.	Vertices	The plural of vertex
5.	Dimension	The size of something in a particular directions e.g. length, width, height, diameter, depth
6.	Plane	A flat 2D surface
7.	Plane of symmetry	When a solid can be cut exactly in half and a part on one side of the plane is an exact reflection of the part on the other side of the plane
8.	Prism	A 3D shape with a uniform cross section
9.	Pyramid	A 3D shape with a polygon as a base and triangular sides that meet at the top
10.	Arc	A section from the circumference (outside) of a circle
11.	Sector	A region of a circle bound by two radii and an arc
12.	Congruent	Exactly the same shape and size e.g. identical
13.	Regular	A shape where all the sides and angles are the same

## Plans and elevations

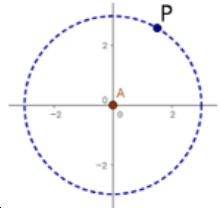
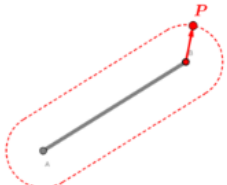
14.	Plan	The view from above a solid	
15.	Front elevation	The view from the front of a solid	
16.	Side elevation	The view from a side of the solid	
17.	Clockwise	Following the direction of a clock	
18.	Anticlockwise	Following the opposite direction of a clock	

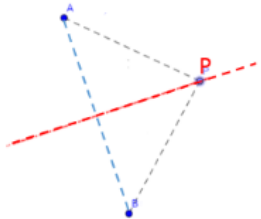
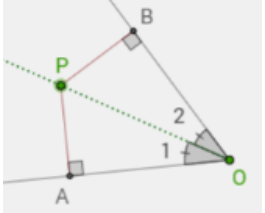
19.	Compass directions	Terminology needed to accurately describe a location or directions	
20.	Sketch	An approximate drawing of an object	
21.	Scale	A ratio that shows the relationship between a length on a drawing/map and the actual length	

## Constructions and loci

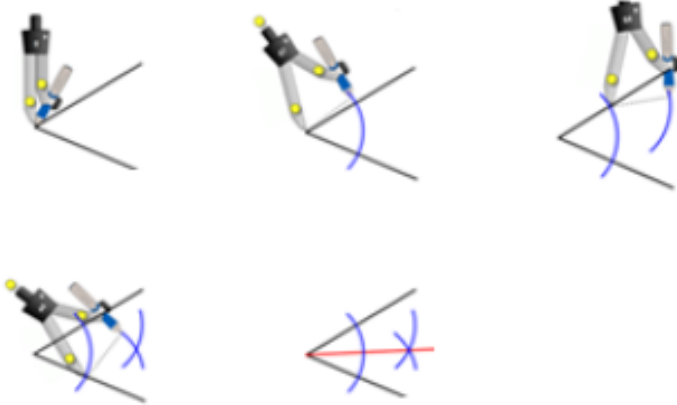
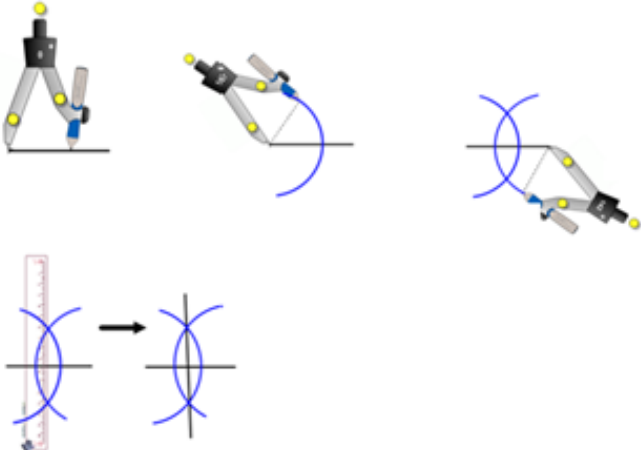
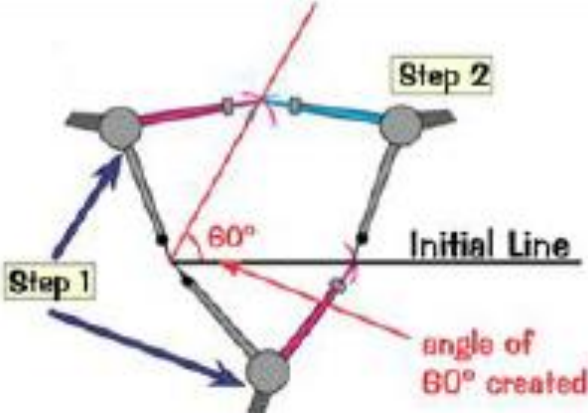
22.	Construct	Draw accurately using a ruler and a pair of compasses.	
23.	Construction lines	Lines or arcs drawn as part of working out	
		They must not be rubbed out as they show the working	
24.	Equidistant	The same distance from each other or in relation to other things	
25.	Bisect	Cut in half	
26.	Perpendicular	At a 90 degree angle (right angle)	
27.	Perpendicular bisector	A line that cuts another in half at a right angle	
28.	Angle bisector	A line that cuts an angle exactly in half	
29.	Locus	The set of all points that fulfil a certain rule	
		Often drawn as a continuous path	
30.	Loci	The plural of locus	
31.	Region	An area bounded by a loci	

## Loci

32.	Circle	Locus of points that are a fixed distance from a fixed point	
33.	Parallel line	Locus of points a fixed distance from a fixed line	

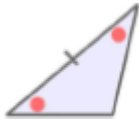

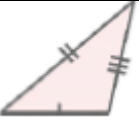

34.	Perpendicular bisector	The line that cuts another in half at a right angle	
35.	Angle bisector	The locus of points equidistant between two fixed points.	

Constructions

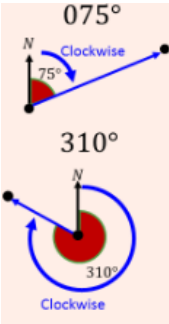
36.	Angle bisector		
37.	Perpendicular bisector		
38.	Constructing 60° angles		

## Constructing triangles

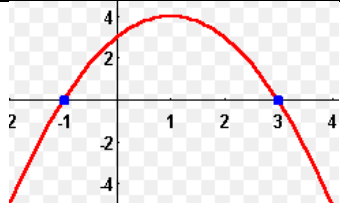
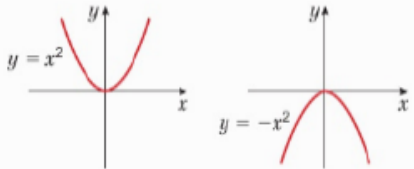
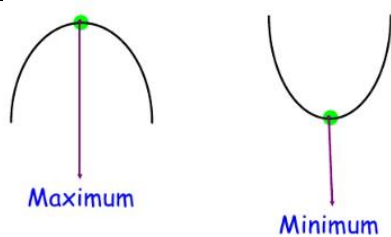
You can draw an accurate triangle when you are given:

39.	ASA	an angle, side, angle	
40.	SAS	a side, angle, side	
41.	SSS	all three sides	
42.	RHS	that it has a right angle, the hypotenuse and another side	

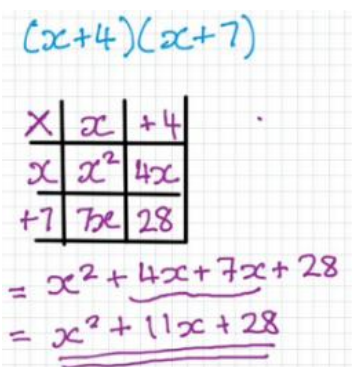
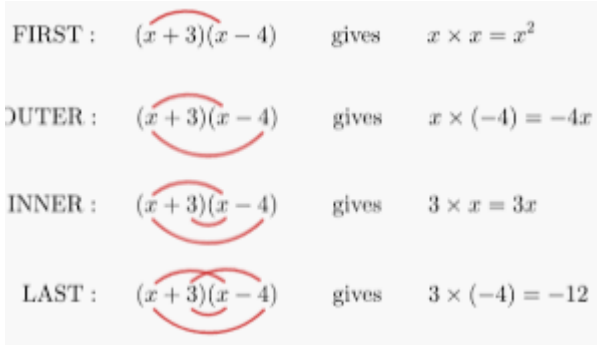
## Bearings

43.	Bearing	The direction of a line in relation to the North-South line	
		It is always measured clockwise	
		Always measured from the North line	
		Always written using 3 digits	

## Quadratics - definitions

1.	Expression	One or a group of terms	
2.	Quadratic expression	An expression where the highest index is 2	e.g. $2x^2 + 2x + 2$
3.	Function	A relation of expression involving one or more variables Also a rule for working out values of y given values for x	
4.	Roots	Solutions to a quadratic equation/function $ax^2 + bx + c = 0$	
		The x values where the graph crosses the x axis	
		A quadratic can have 0, 1 or 2 roots	
5.	Quadratic graph	Curved shaped called a parabola	
		A positive $x^2$ will give a 'U' shape	
		A negative $x^2$ will give a 'n' shape	
6.	Turning points	The point where a curve turns in the opposite direction	
		Can be called a minimum or maximum	

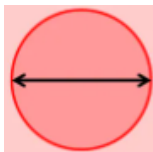
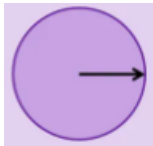
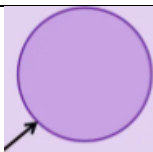
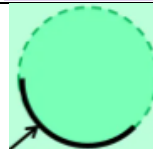
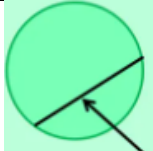
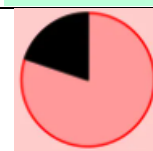

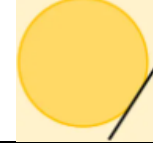
## Expanding double brackets

7.	Everything in the first bracket must be multiplied by everything in the second		
8.	Grid method	FOIL method	
			

## Factorising a quadratic expression

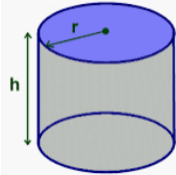
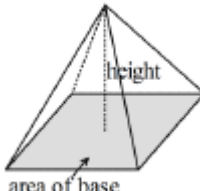
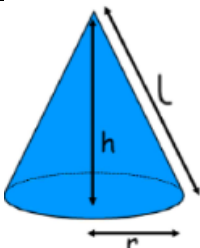

9.	Factorising a quadratic in the form of $ax^2 + bx + c$	<p>Multiply to 5  <math>\swarrow</math>  Factorise <math>x^2 + 5x + 6 \leftarrow</math> Add to 6</p> <p>2 and 3 add to 5  2 and 3 multiply to 6</p> <p><math>(x + 2)(x + 3)</math></p> <p>Check: <math>(x + 2)(x + 3) = x^2 + 5x + 6</math></p>
10.	Difference of two squares	<p>A special type of quadratic which only has two terms.</p> <p>One term is subtracted from the other</p> <div> <math>x^2 - 25 = x^2 - 5^2 = (x + 5)(x - 5)</math>  <math>y^2 - 49 = y^2 - 7^2 = (y + 7)(y - 7)</math>  <math>a^2 - 16 = a^2 - 4^2 = (a + 4)(a - 4)</math> </div>
Solving quadratic equations/functions		
11.	By factorising	<div> <p>Take you factorised form and set each bracket equal to zero</p> <p>Solve each separate linear equation to find the solutions/roots</p> </div> <div> <math>x^2 + 4x + 3 = 0</math>  <math>(x + 3)(x + 1) = 0</math>  <math>\swarrow \quad \searrow</math>  <math>x + 3 = 0 \quad x + 1 = 0</math>  So So  <math>x = -3 \quad x = -1</math> </div>

## Circles - definitions and formulae

1.	Diameter	A straight line from edge to edge passing through the centre	
		Double the size of the radius	
2.	Radius	A straight line from the centre to the edge	
		Half the size of the diameter	
3.	Radii	The plural of radius	
4.	Circumference	Distance around the outside of the circle	
5.	Arc	Part of the circumference	
6.	Chord	A line within a circle where each end touches the edge	
7.	Sector	The region created by two radii and an arc	
8.	Segment	The region created by a chord and an arc	
9.	Tangent	A line outside the circle which only touches the circumference at one point	
10.	Semi -circle	Half a full circle	
Area and circumference of circles formulae			
11.	Pi ( $\pi$ )	Constant ratio linking the circumference and diameter of a circle	
		3.14159265...	

12.	Circumference of a circle	$C = \pi d$	Alternatively, using relationship between $r$ and $d$ $C = 2\pi r$
13.	Arc length	$\frac{x}{360} \times \pi d$	Where $x$ is the angle at the centre
14.	Perimeter of a sector	$\left(\frac{x}{360} \times \pi d\right) + 2r$	This represents the arc length plus the two radii
15.	Area of a circle	$A = \pi r^2$	
16.	Area of a sector	$\frac{x}{360} \times \pi r^2$	

### Cylinders, pyramids, cones and spheres

17.	Volume of a cylinder	$V = \pi r^2 h$	
18.	Surface area of a cylinder	$Total\ surface\ area = 2\pi r^2 + \pi dh$	
19.	Volume of a pyramid	$V = \frac{1}{3} \times area\ of\ base \times perpendicular\ height$	
20.	Volume of a cone	$V = \frac{1}{3} \times \pi r^2 h$	
21.	Surface area of a cone	$Curved\ surface\ area = \pi rl$ $Total\ surface\ area = \pi r^2 + \pi rl$	
22.	Volume of a sphere	$V = \frac{4}{3} \times \pi r^3$	
23.	Surface area of a sphere	$Total\ surface\ area = 4\pi r^2$	



## Fractions

1.	Improper fraction	A fraction where the numerator is larger than the denominator.	e.g. $\frac{4}{3}$
2.	Mixed number	A number made from integer and fraction parts.	e.g. $2\frac{2}{3}$
3.	Unit fraction	A fraction that has a numerator of 1	
4.	Reciprocal	The reciprocal of a number is 1 divided by the number.	e.g. the reciprocal of 3 is $\frac{1}{3}$
		Dividing by a number is the same as multiplying by its reciprocal	e.g. $\times$ by $\frac{1}{3}$ is the same as $\div$ by 3
5.	Convert improper fractions to mixed numbers	<ul style="list-style-type: none"> <li>Divide the numerator by the denominator</li> <li>The answer gives the whole number part.</li> <li>The remainder becomes the numerator of the fraction part with the same denominator.</li> </ul>	$\frac{43}{6} = 7\frac{1}{6}$
6.	Convert mixed numbers to improper fractions	<ul style="list-style-type: none"> <li>Multiply the denominator by the whole number part.</li> <li>Add the numerator to this.</li> <li>Put the answer to this back over the denominator</li> </ul>	$7\frac{1}{6} = \frac{6 \times 7 + 1}{6} = \frac{43}{6}$
7.	Adding and subtracting mixed numbers	<ul style="list-style-type: none"> <li>Convert mixed numbers to improper fractions</li> <li>Transform both fractions so they have the same denominator</li> <li>Add or subtract the numerators</li> <li>Convert back to mixed number if applicable</li> </ul>	
8.	Multiplying mixed numbers	<ul style="list-style-type: none"> <li>Convert mixed numbers to improper fractions</li> <li>Multiply numerators and multiply the denominators</li> <li>Convert back to mixed number if applicable</li> </ul>	
9.	Dividing mixed numbers	<ul style="list-style-type: none"> <li>Convert mixed numbers to improper fractions</li> <li>Flip the second fraction (find the reciprocal)</li> <li>Change the divide sign to a multiply</li> <li>Multiply the fractions</li> <li>Convert back to mixed number if applicable</li> </ul>	

## Index laws

10.	Index	A small number to the upper right of a base number that shows how many times the base number is multiplied by itself.
11.	Power	Another word for an index.
12.	Indices	The plural of index.

13.	Index form	A number written to the power of an index.	
14.	Multiplying	Add the powers	$x^7 \times x^6 = x^{13}$
15.	Dividing	Subtract the powers	$x^5 \div x^6 = x^{-1}$
16.	Brackets	Multiply the powers	$(x^2)^3 = x^6$
17.	Power of 0	Always = 1	$x^0 = 1$
18.	Negative	Means "1 over"	$x^{-n} = \frac{1}{x^n}$
19.	Unit Fraction	Means root	$x^{\frac{1}{n}} = \sqrt[n]{x}$
20.	Fractional	Means root and bracket	$x^{\frac{a}{n}} = (\sqrt[n]{x})^a$

## Standard form

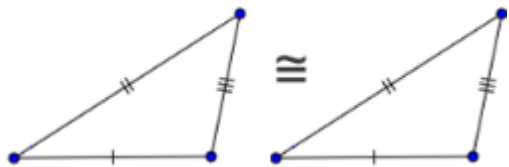
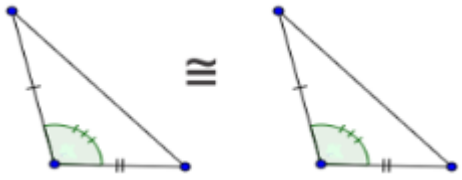
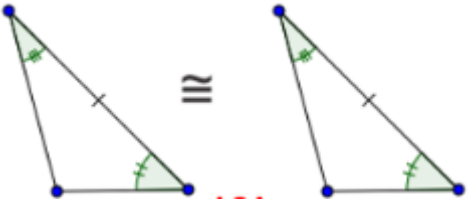

21.	Standard form	A number written in the form: $A \times 10^n$ , where $A$ is between 1 and 10.	
22.	Scientific notation	Another name for standard form	
23.	Convert a small number to standard form	<ul style="list-style-type: none"> <li>Count the number of zero's in front of the first significant figure (including the one in front of the decimal point).</li> <li>The power of ten is negative followed by this number.</li> </ul>	e.g. $0.00000037 = 3.7 \times 10^{-7}$
24.	Convert a large number into standard form	<ul style="list-style-type: none"> <li>Count the number of place value position there are after the first significant figure.</li> <li>The power of ten is positive followed by this number.</li> </ul>	e.g. $147\,100\,000\,000 = 1.47 \times 10^{11}$
25.	Converting to a small ordinary number	<ul style="list-style-type: none"> <li>Look at the digit after the negative in the power of 10.</li> <li>Write this many zero's in front of the first sig. fig.</li> <li>Reposition the decimal place between the first and second zero.</li> </ul>	e.g. $2.4 \times 10^{-6} = 0.0000024$
26.	Adding or subtracting numbers in standard form	<ul style="list-style-type: none"> <li>Convert the numbers to ordinary numbers.</li> <li>Add.</li> <li>Convert the sum to standard form.</li> </ul>	e.g. $(2.3 \times 10^4) + (6.4 \times 10^3) = 23000 + 6400 = 29400 = 2.94 \times 10^4$

27.	Multiplying numbers in standard form	<ul style="list-style-type: none"> <li>• Multiply the numbers between one and 10 at the front.</li> <li>• Use index law for multiplication for the powers of 10.</li> <li>• If necessary increase the power of ten by one to ensure the initial number is between 1 and 10.</li> </ul>	e.g. $(4.5 \times 10^3) \times (3 \times 10^5)$ $= 13.5 \times 10^{3+5}$ $= 13.5 \times 10^8$ $= 1.35 \times 10^9$
28.	Dividing numbers in standard form	<ul style="list-style-type: none"> <li>• Divide the numbers between one and 10 at the front.</li> <li>• Use index law for division for the powers of 10.</li> <li>• If necessary, decrease the power of ten by one to ensure the initial number is between 1 and 10.</li> </ul>	e.g. $(2.5 \times 10^{11}) \div (5 \times 10^{13})$ $= 0.5 \times 10^{-2}$ $= 5 \times 10^{-3}$

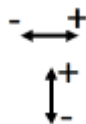
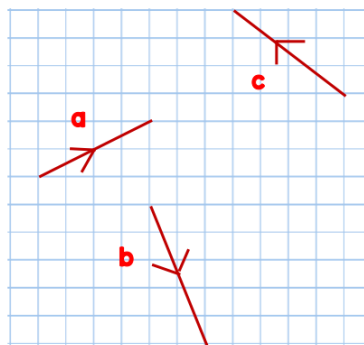
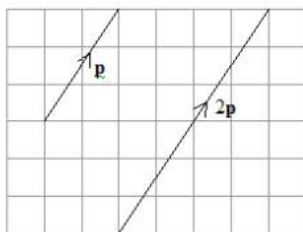
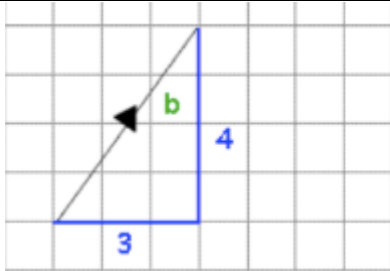
## Similarity and Congruence in 2D

1.	Congruent	Exactly the same shape and size	
2.	Similar	Two shapes where one is an enlargement of another	
		Corresponding angles are equal	Corresponding sides are in the same ratio
3.	Scale factor	The proportion by which the dimensions of an object will increase or decrease by	
4.	Linear scale factor (LSF)	The scale factor/ratio of sides of two similar shapes	$LSF = \frac{\text{length from large shape}}{\text{length from small shape}}$
5.	Area scale factor (ASF)	The scale factor ratio of areas/surface areas of two similar shapes	$ASF = \frac{\text{Area of large shape}}{\text{Area of small shape}}$
6.	Volume scale factor (VSF)	The scale factor/ratio of volumes of two similar shapes	$VSF = \frac{\text{volume of large shape}}{\text{volume of small shape}}$

## Two triangles are congruent if...

7.	SSS	All 3 sides are equal	
8.	SAS	2 sides and the included angle are equal	
9.	ASA	2 angles and the corresponding side are equal	
10.	RHS	The right angle, hypotenuse and one other side are equal	

# Vectors

11.	Magnitude	Size		
12.	Scalar	A quantity has a magnitude		
13.	Vector	A quantity that has direction and magnitude		
14.	Column vector	x denotes the horizontal movement	$\begin{pmatrix} x \\ y \end{pmatrix}$	
		y denotes the vertical movement		
15.	Written vectors	Can be written in bold <b>a</b> or with underlining <u>a</u>		
16.	Vector between two points	A vector between any two given points	e.g. vector between A and B could be written as $\vec{AB}$	
17.		Column vectors can be represented on grids	<div><math>\mathbf{a} = \begin{pmatrix} 4 \\ 2 \end{pmatrix}</math>    <math>\mathbf{b} = \begin{pmatrix} 2 \\ -5 \end{pmatrix}</math>    <math>\mathbf{c} = \begin{pmatrix} -4 \\ 3 \end{pmatrix}</math></div> 	
18.	Adding vectors	$\begin{pmatrix} 2 \\ 3 \end{pmatrix} + \begin{pmatrix} 1 \\ -4 \end{pmatrix} = \begin{pmatrix} 3 \\ -1 \end{pmatrix}$		
19.	Subtracting vectors	$\begin{pmatrix} 2 \\ 3 \end{pmatrix} - \begin{pmatrix} 1 \\ -4 \end{pmatrix} = \begin{pmatrix} 1 \\ 7 \end{pmatrix}$		
20.	Multiplying a vector by a scalar quantity	$\mathbf{p} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$ . Then $2\mathbf{p} = 2 \times \begin{pmatrix} 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 4 \\ 6 \end{pmatrix}$ .		
21.	Magnitude of a vector		<div><math>\mathbf{b} = \begin{pmatrix} 3 \\ 4 \end{pmatrix}</math></div> <div><math>b^2 = 3^2 + 4^2</math> <math>b = \sqrt{3^2 + 4^2}</math> <math>b = 5</math></div>	
22.	Unit vector	Has a magnitude of 1		



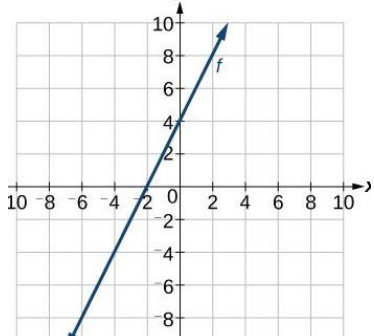
### Algebra definitions

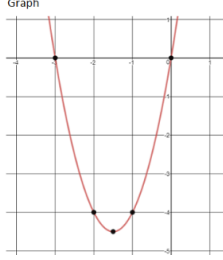
1.	Equation	A mathematical statement containing an equals sign (=) to show that two expressions are equal	
2.	Formula	A rule describing the relationship between different variables	
3.	Formulae	The plural of formula	
4.	Function	A relation involving one or more variables	
5.	Roots	Solutions to an equation	
		In graphs, the values of x where the graph crosses the x axis	
6.	Identity	An equation that is true for any value of x	Denoted using $\equiv$
7.	Substitute	Replace a variable with a number	
8.	Subject	The variable on its own on one side of the equals sign is said to be the 'subject' of a formula	
9.	Rearrange	Change positions of terms using inverse operations	

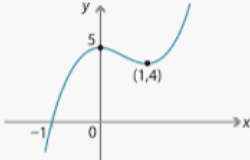
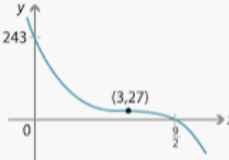
### Changing the subject of a formula (rearranging)

10.	Always use inverse operations to isolate the term you have been asked to make the subject		
	<p>Make <math>u</math> the subject:</p> $v = u + at$ $(-at)$ $v - at = u$ <p>So</p> $u = v - at$	<p>Make <math>u</math> the subject:</p> $v^2 = u^2 + 2as$ $(-2as)$ $v^2 - 2as = u^2$ $(\sqrt{\quad})$ $\sqrt{v^2 - 2as} = u$ <p>So</p> $u = \sqrt{v^2 - 2as}$	



### Types of graphs/functions

11.	Linear	Represented by a straight line	$y = 2x + 4$ 
		Usually represented by $y = mx + c$	
		Can also be given as $ax + by + c = 0$	

12.	Quadratic	General form of $ax^2 + bx + c = 0$	<div>Equation <math>y = 2x^2 + 6x</math></div> <div>Graph </div> <div>Table of Values</div> <table><tr><th>x</th><th>y</th></tr><tr><td>-3</td><td>0</td></tr><tr><td>-2</td><td>-4</td></tr><tr><td>-1</td><td>-4</td></tr><tr><td>0</td><td>0</td></tr><tr><td>1</td><td>8</td></tr></table>	x	y	-3	0	-2	-4	-1	-4	0	0	1	8
		x		y											
		-3		0											
-2	-4														
-1	-4														
0	0														
1	8														
A positive $x^2$ will give a 'U' shape															
A negative $x^2$ will give a 'n' shape															

13.	Cubic	General form of $ax^3 + bx^2 + cx + d = 0$	<div></div> <div>Graph of <math>f(x) = 2x^3 - 3x^2 + 5</math>. <math>b^2 - 3ac = 9</math></div> <div></div> <div>Graph of <math>f(x) = -8(x-3)^3 + 27</math>. <math>b^2 - 3ac = 0</math></div>
		Can have 1, 2 or 3 roots	

14.	Asymptote	A line a graph will get very close to but will not touch
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15.	Reciprocal	General form of $y = \frac{k}{x}$ where k is a number	<div><math>y = \frac{k}{x}</math> (positive)</div> <div></div> <div><math>y = \frac{-k}{x}</math> (negative)</div> <div></div>
		Has two asymptotes	

## Simultaneous equations

16.	Simultaneous equations	Two equations where there are two unknown which have the same value in each
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## Solving simultaneous equations

17.	Elimination	Add or subtract one equation from another to eliminate a variable	
		If the matching coefficients have the same sign then subtract the equations  ✓ Same ✓ Subtract ✓ Substitute	If the matching coefficients have different signs then add the equations  ✓ Different ✓ Add ✓ Substitute
18.	Substitution	Rearrange so the subject of one equation is a single variable	
		Substitute this into the second equation	
19.	Graphically	The points of intersection of two graphs are the solutions to the simultaneous equations	